Research Article

Optical Flow Active Contours with Primitive Shape Priors for Echocardiography

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Accurate delineation of object borders is highly desirable in echocardiography, especially at the left ventricle. Among other modelbased techniques, active contours (or snakes) provide a unique and powerful approach to image analysis. In this work, we propose the use of a new external energy for a *gradient vector flow* (GVF) snake, being the optical flow of a moving sequence (modeling the mechanical movement of the heart). This external energy can provide additional information to the active contour model garnering adequate results for moving sequences. An automatic iterative primitive shape prior was also applied in order to further improve the results of a GVF snake, when dealing with especially noisy echocardiographic images. Results were compared with expert-defined segmentations yielding acceptable sensitivity, precision rate and overlap ratio performance.

1. Introduction

The assessment of cardiac function has been a major area of interest in the medical field. Normal heart function consists of pumping chambers (known as ventricles) which regulate the systemic and pulmonary circulation systems by delivering blood to the proper areas. Detection of nonnormal heart function in the *left ventricle* (LV), for instance, can cause systolic dysfunction, being the reduction in the ability to contract, or diastolic dysfunction, being the inability to fill efficiently. Along with mechanical functions, various heart structures may also fail causing cardiomyopathies, endangering the life of the host individual. Fortunately, many myopathies are treatable (with medication, implanted pacemakers, defibrillators, or ventricular assist devices) given early detection. Echocardiography, imaging the heart using ultrasound waves, facilitates the ability to do so.

The advent of real time ultrasonography provides the ability to image an entire LV and surrounding anatomy within one cardiac cycle (approximately one second). However, depending on the patient's "photogenicity" (impacting factors include and surrounding fatty tissues, calcifications, gender), these images are most likely marred by speckle artifacts. Many computer vision techniques attempt to reduce such speckle noise by means of filtering [1] or incorporating the speckle effect directly into their algorithms [2]. Boundary detection techniques are employed in order to segment the wanted regions for analyses on the heart structures, such as endocardial borders [3], stress and strain of the septum wall [4], and wall motility [5] to name a few.

Various computer vision techniques have been introduced to accomplish boundary detection. Kass el al. [6] first proposed the original active contour model (commonly known as a snake or a deformable model). In their formulation, image segmentation was posed as an energy minimization problem.

Active contours treat the surface of an object as an elastic sheet that stretches and deforms when external and internal forces are applied to it. These models are physically-based, since their behavior is designed to mimic the physical laws that govern real-world objects [7]. Since this approach relied on variational calculus to find a solution, time complexity was one of the main drawbacks of this original model. Amini et al. [8] proposed an algorithm for using dynamic programming, in order to incorporate soft and hard constraints into the formulation, improving time complexity and results. Further improvements to time complexity were proposed by Williams et al. [9], by using a greedy algorithm while



FIGURE 1: Example of gradient vector forces. (a) Standard U-Image. (b) Gradient Vector Flow of U-Image.

incorporating a simple curvature approximation. Issues with large capture ranges and concavities are solved by other advances, which include inflation forces [10], probabilistic models [11], oriented particles [12], and gradient vector flows [13]. For the purposes of this study, focus will be placed on those advances best suited for echocardiographic images.

Since the LV represents one of the most important heart functions, many semiautomatic techniques attempt to segment this region from surrounding tissues [3, 14, 15]. Yet, no universally accepted standard exists for segmenting echocardiographic images.

Papademetris et al. [15] took advantage of a b-splines parameterized deformable model for segmenting cardiac regions. The external energy consisted of the standard intensity term and a *markov random field* (MRF) texturebased term. The MRF is based on a combination of gradient, regional, and curvature data computed from the original image. Initial contours are manually placed for each 2D plane and are passed to a shape tracking algorithm. Displacements are probabilistically computed using a confidence measurement for the entire set. Final displacements are fed into an anisotropic linear elastic model which is computed vis-à-vis a Bayesian estimation framework. The manual placement of the contours makes this technique quite labour intensive.

Felix-Gonzalez and Valedes-Cristerna [14] proposed a segmentation technique for echocardiographic images using an *active surface model* (ASM). The ASM is made up of cubic splines and is based on a gradient descent procedure. When using gradient descent, the empirical setting of parameters is required based on the quality and types of images used. This makes this proposed technique extremely sensitive to its input. Furthermore, Felix-Gonzalez et al.'s work was only tested on two limited datasets.

Leung et al. [16] proposed the use of an *active appearance model* (AAM) and intensity, based registration for segmenting multiple 2D image slices. An AAM uses all the information in an image region covered by the target object, rather than just that near modeled edges. An AAM involves the principal component analysis of the various shapes and textures from several manually segmented 2D slices for training. The AAM makes use of the training set to converge the initial set mesh to the best textures on the image. However, this trained set required several manual segmentations of the 2D image slices to tune it to the medium being used.

The gradient vector flow (GVF) [13] snake was introduced as a modification to the original snake model in order to overcome the capture range and curve concavity issues. However using the GVF snake on echocardiograms directly will not provide an adequate solution due to the complication of speckle noise and the existence of valves within the heart cavity, inhibiting a proper segmentation.

Zhou et al. [17] proposed the segmentation of MRI cardiac sequences using a generalized *fuzzy gradient vector flow* (FGVF) map along with a relative optical flow field. Optical flow measurements are computed on the cardiac sequence being considered, and a *maximum a posteriori probability* (MAP) was used as a window for the movement of the curve. The use of optical flow with GVF provides promising results; however this technique is used exclusively on clear MRI data, and hence the presence of speckle noise on echocardiographic images would require modifications of this technique. Both GVF and optical flow measurements will be used in the proposed technique.

In this paper, we propose to utilize optical flow measurements as an external energy of a GVF snake. We will show that there is ample information in the movement of tissues within the heart cavity that will provide the necessary knowledge to segment out the region of interest. We will further improve the results by providing means of incorporating an iterative prior knowledge process into the proposed solution which takes into account the primitive shape of an object during the active contour evolution cycle. The rest of the paper is organized as follows. Section 2 will outline each module of the proposed model. Section 3 will explain the experimental setup and results, and Section 4 will contain concluding comments.

2. Description of Model

2.1. Parametric Active Contour Review. A snake is an energy minimization problem. Its energy is represented by two forces (internal energy, E_{in} , and external energy, E_{ex}) which work against each other. The total energy should converge to a local minimum—in the perfect case—at the desired boundary. The snake is defined as $v(s) = [x(s), y(s)]^T$, where *s* belongs to the interval [0, 1]. Hence, the total energy to be minimized, E_{AC} , to give the best fit between a snake and a desired object shape is

$$E_{\rm AC} = \int_0^1 E_{\rm in}(\nu(s)) + E_{\rm ex}(\nu(s)) ds.$$
(1)

The internal energy decreases as the curve becomes smooth (by incorporating both elasticity and stiffness), whereas the external energy decreases as approaching the features of interest, such as image structures or edges.

The internal energy of the active contour formulation is further defined as

$$E_{\rm in}(\nu(s)) = \alpha(s) \left| \frac{d\nu(s)}{ds} \right|^2 + \beta(s) \left| \frac{d^2\nu(s)}{ds^2} \right|^2, \qquad (2)$$

where $\alpha(s)$ and $\beta(s)$ are weighting factors of elasticity and stiffness terms, respectively. The first-order term makes the snake's surface act like a membrane. The weight $\alpha(s)$ controls the tension along the spine (stretching a balloon or elastic band). The second-order term makes the snake act like a thin plate. The weight $\beta(s)$ controls the rigidity of the spine (bending a thin plate or wire).

A typical external energy formulation to identify edges for a given image, I(x, y), is

$$E_{\rm ex}(x,y) = - \left| \nabla I(x,y) \right|^2, \tag{3}$$

where ∇ denotes the gradient operator. In the case of a noisier image the edges are further smoothed:

$$E_{\rm ex}(x,y) = -\left|\nabla (G_{\sigma}(x,y) * I(x,y))\right|^2 \tag{4}$$

where $G_{\sigma}(x, y)$ is a two-dimensional Gaussian function with standard deviation σ , and * denotes a convolution operator. Since the contour may get trapped by the noisy areas of the image, σ must be large enough to compensate for the image noise that would interfere with the active contour's capture range. The standard snake algorithm also suffers from poor capture range because initialization and the inability to capture concavities. These problems are largely solved by the advent of the GVF snake [13].

The concavity problem exists due to the gradient vectors in an image generally have large magnitude only in the immediate vicinity of the boundary and are nearly zero at points away from the boundary. As such the capture range of the snake will be quite small. In order to resolve this, the gradient map is extended to points away from boundaries using a computational diffusion process. The GVF field is used as an external energy in the active contour and is characterized by the vector field $z(x, y) = [u(x, y), v(x, y)]^T$ that minimizes the energy functional [13]:

$$E_{\rm GVF} = \iint \mu \left(|\nabla u|^2 + |\nabla v|^2 \right) + \left| \nabla f \right|^2 \left| z - \nabla f \right|^2 dx \, dy,$$
(5)

where *f* is an edge map derived from the image, μ is the degree of smoothness of the field, *u* and *v* characterize the direction and strength of the field. Hence, when $|\nabla f|$ is small, the energy will be dominated by the partial derivates, yielding a slow field. Alternatively, when $|\nabla f|$ is large, the latter term dominates and the function is minimized by setting $z = \nabla f$.

The external energy for the proposed scheme will be generated using a *virtual electric field* (VEF) [18] of f over the traditional GVF technique. Traditional GVF field generation is performed by optimizing the cost function represented in (5), which is quite a time consuming process. The VEF is defined by considering each edge pixel as a point charge within an electric field. This can be accomplished by convolving the edge map with the following two masks:

$$g_{x}(x, y) = \frac{-c \cdot x}{(x^{2} + y^{2})^{3/2}},$$

$$g_{y}(x, y) = \frac{-c \cdot y}{(x^{2} + y^{2})^{3/2}},$$
(6)

where $c = (4\pi\epsilon)^{-1}$ and ϵ is sufficiently small constant. The resulting field yields a vector flow identical to a GVF field, given the masks are large enough. A smaller mask size would ignore outlying edges that would have little impact on the interested features since their range is quite far. However, since echoardiographic images contain many features throughout the image, quantizing any part of the edgemap is not an option. According toPark and Chung [18], an area of radius 32 around the feature should provide adequate flow vectors to accurately recreate a GVF field, without suffering from the high computational cost associated with vector flow generation. Figure 1 illustrates gradient vector forces, where Figure 1(b) shows an example of a vector flow field on the standard U-Image, shown in Figure 1(a), using 65×65 masks generated from (6), which is identical to the original GVF field.

2.2. Optical Flow Review. Optical flow approximates the apparent motion of an object over a series of images (or time). The relationship between the optical flow in the image plane and the velocities of objects in the three-dimensional world is not necessarily obvious [19]. For the sake of convenience, most optical flow techniques consider a particularly simple world where the apparent velocity of brightness patterns can be directly identified with the movement of surfaces in the scene. This implies that objects maintaining structure but changing intensity would break this assumption.

Consider an image intensity I(x, y, t) at time t. Time, in this instance, implies the next frame in an image cine. Assuming that at a small distance away and some time later the given intensity is

$$I(x + \Delta x, y + \Delta y, t + \Delta t)$$

= $I(x, y, t) + \frac{\partial I}{\partial x} \Delta x + \frac{\partial I}{\partial y} \Delta y + \frac{\partial I}{\partial t} \Delta t$ (7)

+ higher order terms.

Given that the object started at position (x, y) at time t, and that it moved by a small distance of $(\Delta x, \Delta y)$ over a period of time Δt , the following assumption can be made:

$$I(x + \Delta x, y + \Delta y, t + \Delta t) = I(x, y, t).$$
(8)

The assumption in (8) would only be true if the intensity of our object is the same at time *t* and $t + \Delta t$. Furthermore, if our Δx , Δy , and Δt are very small, our higher-order terms would vanish, that is,

$$\frac{\partial I}{\partial x}\Delta x + \frac{\partial I}{\partial y}\Delta y + \frac{\partial I}{\partial t}\Delta t = 0.$$
(9)

Dividing (9) by Δt will yield

$$-\frac{\partial I}{\partial t} = \frac{\partial I}{\partial x}\frac{\Delta x}{\Delta t} + \frac{\partial I}{\partial y}\frac{\Delta y}{\Delta t},$$
(10)

$$-I_t = \frac{\partial I}{\partial x}u + \frac{\partial I}{\partial y}v, \quad \text{where } u = \frac{\Delta x}{\Delta t}, \ v = \frac{\Delta y}{\Delta t}.$$
(11)



FIGURE 2: Example of an optical flow field on a Rubik's cube rotated image. (a) Cube at time *t*. (b) Cube at time $t + \Delta t$. (c) Optical flow of image (a) to (b) using Lucas-Kanade method (Originally published inRussell and Norving [22]).



FIGURE 3: Generation of primitive priors on the active contour.

Equation (11) is known as the optical flow constraint equation, where I_t , at a particular pixel location (x, y), is how fast its intensity at this location is changing with respect to time: u and v are the spatial rates of change for any given pixel (i.e., how fast an intensity is moving across an image). However, effectively estimating the component of the flow (along with intensity values) cannot directly be solved in this form since it will yield one equation per pixel for every two unknowns, u and v. In order to do so, additional constraints must be applied to this equation.

Lucas and Kanade [20] and Horn and Schunck [21] introduced two common methods for solving this problem using partial derivatives. The former assumes that the flow field is locally smooth (for a given static window size) and then solves (11) by means of a least squares approximation technique. The latter uses a global regularization parameter which assumes that images consist of objects undergoing rigid motion, resulting in a smooth optical flow over a relatively large area. Figure 2 depicts a visual representation of the optical flow of a simple Rubik's cube. Notice that the grayscale image has few shadows, helping to maintain consistency in the luminance of each pixel, hence yielding accurate results. When dealing with noisy echocardiograms, a global regularization parameter will deal with the speckle better than the static window. This is due to the speckle noise remaining relatively static, lacking fluidity, throughout an image. Hence, the speckle will be "filtered", since the optical flow calculations will fail to realize it within the frames.

Optical flow magnitudes will be combined with the image's edge maps (Section 2.4) in order to generate the external energy in (1) of the GVF snake. This would help to reduce artifacts due to static speckle noise, while also providing more information for the contour points to track (i.e., the tissue mass movement).

2.3. Primitive Shape Prior Knowledge. Since we are dealing with structures that have known shapes and sizes, and many real world models have been already measured, prior knowledge information can be directly used to increase the performance of a segmentation algorithm. Priors based on shape statistical models require modifications to the standard active contour model. An iterative solution can be incorporated directly into any optimization model by using the proposed framework which we first outlined in Hamou et al. [23].

Since it is desirable to incorporate shape priors without directly involving the user for training, automatic shape detection takes place on the set of discrete snake points v(s). This is achieved by first generating the least squares fit polynomial(s) of the current v(s) points. For our left ventricle application, snake points are divided into an upper region and a lower region, which will be approximated by two separate third-order hyperbolas. These hyperbolas will better suit the shape of the left ventricle during both systole and diastole, though any shape prior can be represented by means of simple primitives. Least squares fitting technique is utilized to estimate the two hyperbolas coefficients. The axis separating the two regions is computed by taking the two-thirds upper and one-third lower bounds on all snake points. This separator can be tuned by shifting it upwards or downwards (either manually by the user or automatically by the system) in order to minimize the distance between the fitted hyperbolas and snake points. Priors are then generated by joining the fitted primitives to form one solid shape.



FIGURE 4: Top-level flow chart of the algorithm.

Primitives are bounded by the furthest easterly and westerly points by the snake points, in order to prevent the possibility of a nonconnecting shape.

Once the priors have been generated, its GVF field is computed. This new field will replace the existing external energy of the GVF snake for this specific snake iteration. Figure 3 portrays the process of generating a primitive prior for the left ventricle of the 4-chamber view image, where two intersecting hyperbolas are used (default shape for our left ventricle application).

The fitting of a primitive shape (or a series of primitives as needed for the left ventricle) to the snake points, v(s), will help compensate for the noise that inhibits the snake from migrating past a certain point. It will also help retract the snake towards the primitive prior when an occluded border exists, common in many echocardiographic images. The user can control the number of cycles between any two consecutive prior calculation cycles (prior step parameter). This allows for the increase or decrease in the inherent effect of the prior knowledge to the snake's convergence cycle. This primitive prior module is useful in the medical arena where the specialist or clinician has a clear understanding of the underlying structure being detected, such as a liver, an artery, or a heart. They can choose their desired primitive shape (or series of shapes) before curve evolution takes place.

2.4. Complete System. Figure 4 illustrates a top-level block diagram of the proposed system. It starts with the calculation of the optical flow magnitude on the image cines (*as explained in Section* 2.2). The estimated optical flow is preprocessed by median filtering. A Canny edge map of the filtered optical flow magnitude was generated and added to the original image edge map following normalization. The Canny detector was applied due to its use of nonmaximum suppression that further aids in the filtering of speckle noise. This result is used to generate the GVF for the snake's external energy. GVF snake evolution (*as explained in Section* 2.1) iterates to further minimize the energy function until a prior cycle condition is satisfied (*as explained in Section* 2.3), at which the prior cycle is initiated. At the prior cycle, a GVF is



FIGURE 5: Optical flow fields on the left ventricle using Lucas-Kanade and Horn-Schunck methods.

generated from the prior and a single optimization iteration of the snake is executed before returning to the non-prior original snake iteration. This process is repeated until the snake is optimized and equilibrium is achieved.

3. Experimental Results

For this study, a series of B-mode echocardiogram cross sectional videos of the heart have been used to investigate the proposed snake algorithm. These videos were acquired using an SONOS 5500 by Philips Medical System. The transducer frequency was set at 2.5 Mhz in order to insure adequate penetration of tissue, while maintaining good image quality. Longitudinal views of the heart, which nicely visualize the left ventricle, were acquired. The generated videos were treated as sears of individual images in sequence.

For optical flow calculations, both Horn-Schunck and Lucas-Kanade were able to represent the motion of the heart, though Lucas-Kanade showed a greater number of scatter errors due to its local estimation of regions. As shown in Figure 5(a), at lower local window sizes, the low-level structure information was not represented. In Figure 5(b), where the window size is 5×5 , noise starts to cloud the left ventricle structure, and in Figure 5(c), where the window size is 15×15 , all information is lost by the noise. The high amount of speckle inherent to US images made it difficult to cope. The Horn-Schunck technique, with a global regularization parameter λ between 0.05 and 0.09, was able to compensate for the general speckle throughout the

US images while maintaining structural endocardial lining. Empirically, we found that smoothing greater than this, as exhibited in Figure 5(d), where $\lambda = 0.001$, would start to erode structural feature borders. Smoothing less than this, as exhibited in Figure 5(f), where $\lambda = 1.00$, would result in scatter and false flow measurements due to the noise. For this application, a regularization parameter of 0.07 was selected.

The mask size for generating the GVF field was set to 65 by 65 in order to calculate the point charges and is then normalized for active contour use. For left ventricle segmentation, the initial contour was set to be a small oval (of radius greater than 30 pixels along its minor axis and 60 pixels along its major), which was placed by the user within the left ventricle of the heart on the first image cine. Following image in the sequence would grab the previous segmented left ventricle contour and use it as its initial contour. Hence each dataset (or set of image sequences) was only initialized once.

Snake parameters α and β were set to 4.0 and 0, respectively. β was set to 0 due to the influence of the prior knowledge component which offsets the curvature, whereas α was set to 4.0 in order to make sure that the external and internal energies were neatly balanced. The prior step parameter was set to 5. By decreasing the value of this step parameter, greater shape regularity would occur, but it would take much longer for the snake to reach equilibrium. Empirically, we found that a prior step parameter of 5 was balanced enough to maintain the shape regularity of the snake, without greatly affecting the time complexity.



FIGURE 6: Example of a left ventricle segmentation using the proposed scheme. (a)-(j) Prior formulation steps, where the prior step parameter is set at every five iterations of energy optimization process. (k) and (l) represent the final segmentation of the left ventricle with and without utilizing shape priors, respectively.

During our experimentations, we assumed that equilibrium is achieved when there is less than 10% movement of contour points throughout the snake between two consecutive snake evolutions.

Since the proposed model is iterative, other adjustments can be made during the prior knowledge phase, such as increasing internal energy weights dependent on the distance of fitted priors to snake curve and other various optimizations without upsetting the actual active contour model, though none were done for the purposes of this experiment.

Figure 6 shows an example of a left ventricle segmentation using the proposed scheme. Figures 6(a)-6(j) illustrate the outcome of the proposed active contour iterations, where the prior step parameter is set to five iterations (in order to demonstrate the contour progression over the cycle). Figure 6(k) represents the final contour when utilizing the shape priors and the optical flow as an external energy. Figure 6(1) shows the final contour when utilizing the optical flow as an external energy exclusively without shape priors. Examination reveals that the shape priors helped to maintain shape regularity and properly delineate the left ventricular endocardial lining, despite being disrupted by the speckle noise, artifacts, and valves movements.

Experiments were run on eight complete cardiac cycles from different patients. The performance of the proposed system was measured by comparing 130 indexed segmented image cines from the eight cardiac cycles to the manually delineated segmentations by an expert radiologist, representing the gold standard used.

Since the images at hand were mainly small segmented foregrounds (left ventricular surface area) against vast backgrounds, the system performance would best be measured by means of its *sensitivity*, *precision rate*, and *overlap ratio*. Let us consider the following metrics: a *true positive* pixel is a pixel that is considered part of the left ventricle by both of the



FIGURE 7: Example of segmenting a heart left ventricle. (a) Original left ventricle ultrasound image, (b) expert manual segmentation, (c) segmentation using standard GVF, (d) segmentation using GVF-optical flow without priors, and (e) segmentation using the proposed GVF-optical flow with priors.

proposed method and the gold standard. A false positive pixel is a pixel that is considered part of the left ventricle by the proposed method but it is not considered as such on the gold standard. A false negative pixel is a pixel that is not considered as part of the left ventricle by the proposed method; yet it is considered to be part of the ventricle according to the gold standard. The sensitivity is the percentage of the number of true positive pixels divided by the sum of the number of true positive pixels, and false negative pixels. In other words, it classifies how well a binary classification test correctly identifies a condition. Precision rate is the percentage of the number of true positive pixels divided by the sum of the number of true positive pixels and false positive pixels. In other words, it classifies how accurate the results of the test when the results are positive. Overlap ratio is the percentage of the number of true positive pixels divided by the sum of the number of true positive pixels, false positive pixels and false negative pixels.

The sensitivity, precision rate, and overlap ratio of the proposed system on the 130 segmented cines can be seen in Table 1. This was generated by combining the total metric aggregates across all 130 cines, and calculating the sensitivity, precision rate and overlap ratio measures. In comparison, the standard GVF snake's on the same dataset yields an adequate sensitivity this is due to over-segmentation by the GVF method, since the speckle tends to complicate image features. When optical flow is added to the GVF model some

of the inherent noise is filtered out (due to the static nature of the speckle); hence the segmentation results are improved. By using primitive priors to help the snake's regularity, results are further improved (as revealed in Table 1).

Figure 7 illustrates the segmentation of a heart left ventricle using various segmentation schemes. Figure 7(a) shows the original left ventricle of the heart ultrasound image, whereas Figure 7(b) shows an expert manual segmentation of the image shown in Figure 7(a). Figure 7(c) depicts the final contour using the original GVF snake model (yielding a sensitivity, precision rate and overlap ratio of 71.9%, 96.3% and 70.0%, resp.). Figure 7(d) shows the results of using optical flow GVF without priors (yielding 80.7%, 93.9%, and 76.7%). Figure 7(e) shows the final contour using our optical flow GVF snake with primitive priors (yielding a sensitivity, precision rate, and overlap ratio of 85.2%, 91.9%, and 79.2%, resp.). Examination of the figure reveals that the shape priors improve regularity by allowing the snake to overcome noise artifacts. This allows for proper delineation of the left ventricular endocardial lining. The standard GVF's precision rate is slightly higher in this example, since the GVF contour results in a severely under segmented region, hence having very few false positives. In our scheme, the motion information (optical flow) is used as structural information in the external energy of the snake. This motion information ignores much of the speckle, due to its static nature, preventing feature under segmentation.

TABLE 1: Sensitivity, precision rate, and overlap ratio of the proposed segmentation system.

• • • • •		
ensitivity	Precision rate	Overlap ratio
90.4%	70.2%	65.3%
92.8%	76.5%	72.2%
93.7%	80.9%	76.7%
	90.4% 92.8% 93.7%	ensitivity Precision rate 90.4% 70.2% 92.8% 76.5% 93.7% 80.9%

4. Concluding Remarks

In this paper, we have shown that optical flow can be utilized as an external energy within the GVF active contour framework. We have demonstrated that an active contour method is able to make use of the knowledge derived from the apparent motion of tissue via optical flow measurements. This strengthens the principle that tissue movement should be considered within segmentation techniques, where the data facilitates it.

Furthermore, results were improved by using primitive shapes, which helped overcome the inherent difficulties in segmenting echocardiographic images, by maintaining shape regularity. The proposed prior technique does not require training samples that are expert delineated; rather they are built from the current active contour control points. Furthermore, different primitive priors can be used depending on the feature of interest to be segmented. Such segmentations would improve the calculation of various clinical measures by reducing the inconsistencies and variability between clinicians while simultaneously reducing the time for clinician interaction.

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