

# On-Line Selection of Discriminative Tracking Features <sup>\*</sup>

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## Abstract

*This paper presents a method for evaluating multiple feature spaces while tracking, and for adjusting the set of features used to improve tracking performance. Our hypothesis is that the features that best discriminate between object and background are also best for tracking the object. We develop an on-line feature selection mechanism based on the two-class variance ratio measure, applied to log likelihood distributions computed with respect to a given feature from samples of object and background pixels. This feature selection mechanism is embedded in a tracking system that adaptively selects the top-ranked discriminative features for tracking. Examples are presented to illustrate how the method adapts to changing appearances of both tracked object and scene background.*

## 1. Introduction

Two decades of vision research have yielded an arsenal of powerful algorithms for object tracking. Moving objects can be effectively tracked in real-time from stationary cameras using frame differencing or adaptive background subtraction combined with simple data association techniques [11]. This approach can be generalized to situations where the video data can be easily stabilized, including purely rotating and zooming cameras, and aerial views where scene structure is approximately planar [5]. Modern appearance-based tracking methods such as the mean-shift algorithm use viewpoint-insensitive appearance models to track objects through non-rigid pose changes without any prior knowledge of scene structure or camera motion [4]. Kalman filter extensions achieve more robust tracking of maneuvering objects through the introduction of statistical models of object and camera motion [2]. Particle filtering extensions enable tracking through occlusion and clutter by reasoning over a state-space of multiple hypotheses [6].

Our experience with a variety of tracking methods can be summarized simply: tracking success or failure depends primarily on how distinguishable an object is from its sur-

roundings. If the object is very distinctive, we can use a simple tracker to follow it. If the object has low-contrast or is camouflaged, we will obtain robust tracking only by imposing a great deal of prior knowledge about scene structure or expected motion, and thus tracking success is bought at the price of reduced generality.

The degree to which a tracker can discriminate object and background is directly related to the feature space(s) used. Surprisingly, most tracking applications are conducted using a fixed set of features, determined apriori. Sometimes, preliminary experiments are run to determine which fixed feature space to use – a good example is work on head tracking using skin color, where many papers evaluate different color spaces to find one in which pixel values for skin cluster most tightly, e.g. [14]. However, these approaches ignore the fact that it is the ability to distinguish between object and background that is most important, and the background can not always be specified in advance. Furthermore, both foreground and background appearance will change as the target object moves from place to place, so tracking features also need to adapt. Figure 1 illustrates this with low contrast imagery of a car traveling through patches of sunlight and shadow. The best feature for tracking the car through sunlight performs poorly in shadow, and vice versa.

A key issue addressed in this work is on-line, adaptive selection of an appropriate feature space for tracking. Our insight is that the feature space that best distinguishes between object and background is the best feature space to use for tracking, and that this choice of feature space will need to be continuously re-evaluated over time to adapt to changing appearances of the tracked object and scene background. Target tracking is cast as a local discrimination problem with two classes: foreground and background. This point of view opens up a wide range of pattern recognition feature selection techniques that can be adapted for use in tracking. An interesting characteristic of target tracking is that foreground and background appearances are constantly changing, albeit gradually. Naturally, when class appearance varies, the most discriminating set of features also varies [9]. The issue of on-line feature selection has rarely been addressed in the literature, especially under the hard constraint of speed required for target tracking. The nearest

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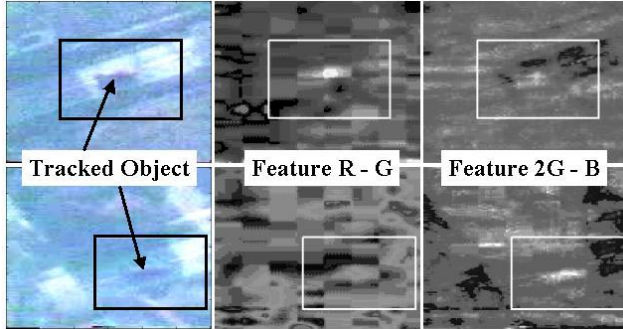


Figure 1: Features used for tracking an object must be adapted as the appearance of the object and background changes. The source imagery (left column) is low contrast aerial video of a car on a road. The car travels between sunny patches (top row) and shadow (bottom). The best feature for tracking the car in sunlight (R-G) performs poorly in shadow. Similarly, the best feature for tracking through shadow (2G-B) does not perform as well in sunlight.

relevant work is [12], which dynamically switches between five color spaces to improve face tracking performance.

Section 2 presents a brief look at off-line discriminative feature selection in the field of pattern classification. Section 3 adapts these ideas to the task of target tracking. Since the goal is to perform on-line feature selection while tracking, efficiency must be favored over optimality. Examples are presented in Section 4 to illustrate how incorporating feature selection with tracking facilitates adaptation to changing object and background appearance.

## 2. Feature Selection

Feature selection is a technique for dimensionality reduction whereby a set of  $m$  features is chosen from a pool of  $n$  candidates, where usually  $m \ll n$  [1]. This technique can be used to rule out irrelevant or redundant features to improve classification performance.

The two main components in feature selection are the selection criterion function, which is a quantitative measure used to compare one feature subset against another, and the search strategy, which is a systematic procedure to enumerate candidate feature subsets and to decide when to stop. Criterion functions can be categorized by whether the evaluation process is data intrinsic (filters) or classifier-dependent (wrappers). For discrimination problems, the criterion involves evaluation of the discriminating power of the selected feature subset. There are many ways to evaluate the discriminative power of each feature. For example, augmented variance ratio (AVR) has been shown to be effective for feature ranking as a preprocessing step for feature subset selection [7, 8, 9]. AVR is the ratio of the between class variance of the feature to the within class variance of the feature. Other measures for discriminative power of a fea-

ture include information gain and mutual information.

The goal in feature subset selection is to find  $m$  features that best complement each other for the classification task at hand. Since we usually do not know what the best subset size  $m$  should be, the search space for feature subsets is  $2^n$ , where  $n$  is the total number of features. Existing heuristic search methods for feature selection provide a set of compromises between speed and optimality. For example, Sequential Forward Selection [1] has a linear computational complexity in  $n$ , but its greedy strategy can result in suboptimal feature sets. In biomedical imaging, a combination of feature ranking and feature subset selection has been shown to be effective for off-line selection of discriminative subsets from thousands of feature candidates [8]. To achieve on-line selection, we are forced to consider simplified selection criteria, non-exhaustive search spaces and heuristic search strategies. In this work, we simplify by finding the best  $m$  features individually, fully realizing that the best  $m$  individual features may not form the best feature subset of size  $m$  [13].

## 3. Feature Selection for Tracking

Our goal in this section is to develop an efficient method that continually evaluates and updates the set of features used for tracking. Our hypothesis is that the most promising features for tracking are the same features that best discriminate between object and background classes. Given an appearance model learned from previous views of the object, the distribution of feature values for object and background samples is computed. Candidate features are then rank-ordered by measuring separability of the distributions of object and background classes. The most discriminative features are used to weight pixels in a new video frame with the likelihood that they correspond to either object or background. Discriminative features produce likelihood maps where object pixels have high values, and background pixels have low values. We use the mean-shift algorithm as a non-parametric method to find the nearest local mode of this likelihood surface, thereby estimating the 2D location of the object in the image.

It is important to note that the features we use for tracking need only be *locally* discriminative, in that the object only needs to be clearly separable from its immediate surroundings. This is a much less restrictive assumption than is necessary for a tracker that uses a fixed set of features, since that set must by necessity be discriminative across a wide-range of imaging conditions. Since we are swapping features in and out on the fly while tracking, we are able to focus on finding features that are finely-tuned to provide good foreground/background discrimination, even if they are only locally, and temporarily, valid.

### 3.1 Feature Spaces

In principle, a wide range of features could be used for tracking, including color, texture, shape and motion. Each potential feature space typically has dozens of tunable parameters, and therefore the full set of potential features that could be used for tracking is enormous. In this work, we represent target appearance using histograms of color filter bank responses applied to R, G, B pixel values within local image windows. This representation is chosen since it is relatively insensitive to variations in target appearance due to viewpoint, occlusion and non-rigidity. Although we only consider color features in this paper, the approach can be extended to incorporate other cues such as texture.

The set of candidate features is composed of linear combinations of camera R,G,B pixel values. Specifically, for our experiments, we have chosen the following set of feature-space candidates

$$F_1 \equiv \{w_1R + w_2G + w_3B \mid w_* \in [-2, -1, 0, 1, 2]\} \quad (1)$$

that is, linear combinations composed of integer coefficients between -2 and 2. The total number of such candidates would be  $5^3$ , but by pruning redundant coefficients where  $(w'_1, w'_2, w'_3) = k(w_1, w_2, w_3)$ , and by disallowing  $(w_1, w_2, w_3) = (0, 0, 0)$ , we are left with a pool of 49 features. This set of candidate features is chosen because: 1) the features are efficient to compute (only integer arithmetic is involved); 2) the features approximately uniformly sample the set of 1D subspaces of 3D RGB space; and 3) some common features from the literature are covered in the candidate space, such as raw R, G and B values, intensity R+G+B, approximate chrominance features such as R-B, and so-called *excess* color features such as 2G-R-B.

All features are normalized into the range 0 to 255, and further discretized into histograms of length  $2^b$ , where  $b$  is the number of bits of resolution. We typically discretize to 5 or 6 bits, yielding feature histograms with 32 or 64 buckets. This discretization is performed for efficiency, and for defeating the “curse of dimensionality” when trying to estimate feature densities from small numbers of samples.

### 3.2 Evaluating Feature Discriminability

If both object and background were uni-colored, then a plausible argument could be made that variation in apparent color of pixels would lead to Gaussian distributions in color space. In this case, Linear Discriminant Analysis (LDA) could be used to find the subspace projection yielding the least overlap (i.e. maximum separability) between object and background. However, we must be able to handle targets and backgrounds that have multi-modal distributions of colors. These violate LDA’s Gaussian assumption, and thus invalidate its analytic solution.

Our approach is to empirically evaluate all candidate features to determine which ones yield good class separability. For a given feature, we measure separability between the object and background classes by 1) estimating the distributions of object and background pixels with respect to the feature; 2) computing the log likelihood ratio of these distributions; and 3) applying a *variance ratio* measure to the distribution of likelihood values from object vs background. Figure 2 illustrates this process.

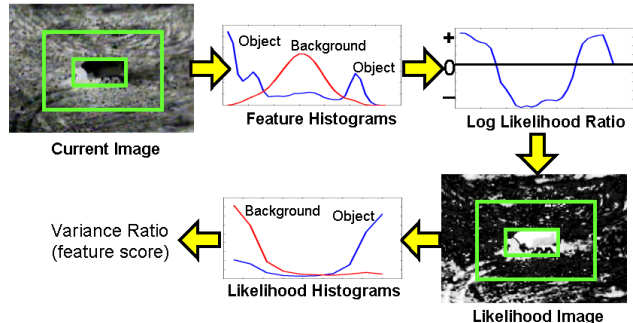


Figure 2: Empirical evaluation of a candidate feature, demonstrated on an IR image of a truck. Histograms of (possibly multi-modal) feature values for object and background pixels are used to compute a log likelihood function in which object pixels have unimodally positive values and background pixels have unimodally negative values. When mapped back into image space, the result is a 2D “likelihood” image that can be used to track the object. The variance ratio is computed from histograms of these likelihood values for object and background pixels to determine separability of the two classes, which correlates well with suitability of the likelihood image for tracking.

We use a “center-surround” approach to sampling pixels from the object and the background. That is, a compact set of pixels (e.g. rectangle or ellipse) covering the object is chosen to represent the object pixels, while a larger surrounding ring of pixels is chosen to represent the background. This is a conservative strategy that leads to discriminative features that separate object from background regardless of which direction the object maneuvers in the image. Of course, we could sample background appearance in other ways. For example, we could bias selection of pixels from the area of the image that we expect the object to traverse in the future, given its recent trajectory.

Given a feature  $f$ , let  $H_{obj}(i)$  be a histogram of that feature’s values for pixels on the object, and  $H_{bg}(i)$  be a histogram for pixels from the background sample, where index  $i$  ranges from 1 to  $2^b$ , the number of histogram buckets. We form an empirical discrete probability density  $p(i)$  for the object, and density  $q(i)$  for the background, by normalizing each histogram by the number of elements in it.

The log likelihood of a feature value  $i$  is given by

$$L(i) = \log \frac{\max \{p(i), \delta\}}{\max \{q(i), \delta\}} \quad (2)$$

where  $\delta$  is a small value (we set it to 0.001) that prevents dividing by zero or taking the log of zero. The nonlinear log likelihood ratio maps potentially multimodal object/background distributions into positive values for colors distinctive to the object, and negative for colors associated with the background. Colors that are shared by both object and background tend towards zero. A new image composed of these log likelihood values becomes the ‘‘likelihood’’ image used for tracking (Figure 2).

Finally, we compute the variance ratio of  $L(i)$  in order to quantify the separability of object and background classes under feature  $f$ . Given a discrete probability density function  $a(i)$ , we use the equality  $\text{var}(x) = Ex^2 - (Ex)^2$  to define the variance of  $L(i)$  with respect to  $a$  as

$$\text{var}(L; a) = E[L^2(i)] - (E[L(i)])^2 \quad (3)$$

$$= \sum_i a(i)L^2(i) - [\sum_i a(i)L(i)]^2. \quad (4)$$

The variance ratio of the log likelihood function can now be defined as

$$\text{VR}(L; p, q) \equiv \frac{\text{var}(L; (p+q)/2)}{[\text{var}(L; p) + \text{var}(L; q)]} \quad (5)$$

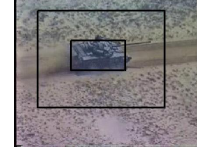
which is the total variance of  $L$  over both object and background pixels, divided by the sum of the within class variances of  $L$  for object and background treated separately.

The intuition behind the variance ratio is that we would like log likelihood values of pixels on both the object and background to be tightly clustered (low within class variance), while the two clusters should ideally be spread apart as much as possible (high total variance). The denominator enforces that the within class variances should be small for both object and background classes, while the numerator rewards cases where values associated with object and background are widely separated. Note the similarity to the Fisher discriminant used in the computation of LDA, where the squared difference between the mean values of the two classes is used as an alternative measure of total variance.

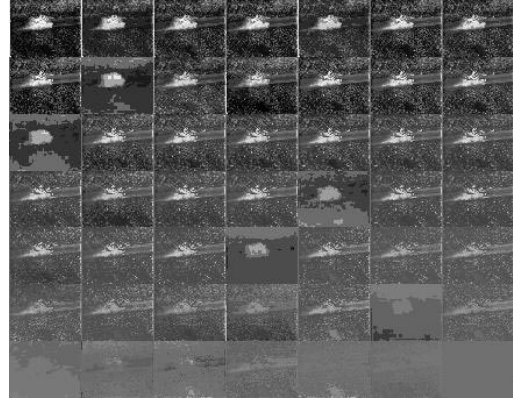
### 3.3 Ranked Likelihood Images

If a feature’s two-class log likelihood function from the previous step is used to label pixels in a new video frame, the result is a likelihood image where, ideally, object pixels contain positive values and background pixels contain negative values. Figure 3 shows a sample object, and the set of likelihood images produced by all 49 candidate features, after rank-ordering the features based on the two-class variance ratio measure. The likelihood image for the most

discriminative feature is at the upper left, and the image for least discriminative feature is at the lower right. We observe a very high correlation between variance-ratio ranking and suitability of the likelihood image for localizing the object in the next frame.



(A)



(B)

Figure 3: (A) A sample image with concentric boxes delineating object and background samples. (B) Likelihood images produced by all 49 candidate feature spaces, rank-ordered by the two-class variance ratio measure. The likelihood image for the most discriminative feature (which is also best for tracking) is at the upper left. The image for least discriminative feature (worst for tracking) is at the lower right.

Figure 4 shows other sample images with labeled object and background pixels, along with log likelihood images associated with the features having highest, median, and lowest variance ratio values, corresponding to the best, median and worst features, respectively, in terms of object/background separability. Again, we see good agreement between these rankings and our intuitive preference regarding which likelihood images to use for tracking.

### 3.4 Tracking

The above feature ranking mechanism is embedded in a tracking system as depicted in Figure 5. Object pixels and background pixels are sampled from the current frame, given the current location of the tracked object. Potential tracking features are ranked using the variance ratio of log likelihood values to determine how well each feature distinguishes object from background in the current frame. The top  $N$  most discriminative individual features are used to compute likelihood images for the next frame ( $N = 5$  for

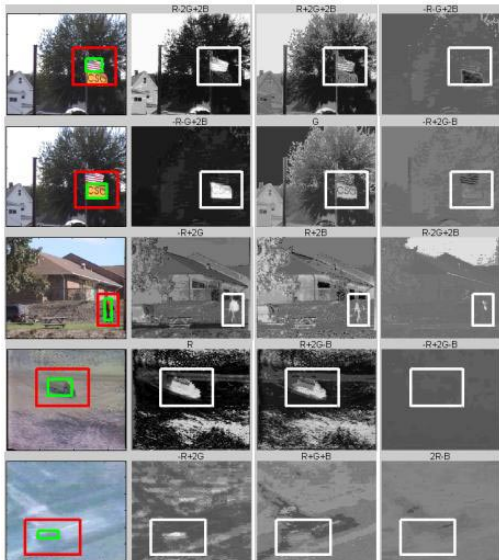


Figure 4: Sample video frames with ranked likelihood images. Left column: frame with labeled object (green box) and background pixels (red box) pixels. Second-fourth columns: likelihood images corresponding to the highest ranked, median, and lowest ranked features, respectively. We can see that rank ordering features by two-class variance ratio correlates well with intuition regarding which features would be best to use for tracking the object.

the experiments shown in the next section). Due to the continuous nature of video, the distribution of object and background features in the next frame should remain similar to the current frame, and thus the most discriminative features should still be valid. A local mean-shift process is initialized in each of the  $N$  new likelihood images. These processes perform gradient ascent to find the nearest local mode in their respective likelihood images. These mean-shift processes converge to  $N$  estimates of the 2D location of the object in the frame, which are combined to yield a new estimate of object location.

The algorithm iterates through each subsequent frame of the video, extracting new samples of object and background pixels, and choosing new sets of discriminative features. In this way, both the features used for tracking and the appearance models of object and background classes evolve together over time. Adaptively updating appearance models in this manner raises the specter of *model drift*, a classic problem in adaptive tracking. Model drift builds up gradually over time as misclassified background pixels start to “pollute” the foreground model, leading to further misclassification and eventual tracking failure. To avoid this problem, we enforce our empirical object density function at the current frame to be a combination of the current observed density and the original training density from the first frame, which is assumed to be uncontaminated. This allows the

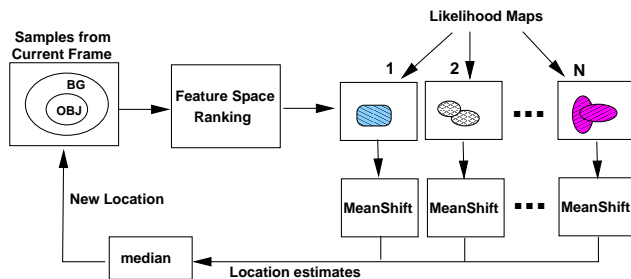


Figure 5: Overview of tracking system with on-line, adaptive feature selection. Samples of object and background pixels in the current frame guide evaluation of candidate features, leading to a rank ordering of features based on discriminative ability. The top  $N$  best features are applied to the next frame to compute likelihood images. A mean-shift process is applied to each likelihood image to compute a 2D location estimate. These estimates are pooled to determine the best location of the object in the new frame, and the procedure iterates.

object appearance model to expand to adapt to current conditions, while keeping the overall density anchored to the original training appearance of the object. This heuristic approach assumes that the object appearance will not change drastically over the tracking sequence.

## 4. Experiments

In this section we present two challenging tracking examples that illustrate the benefits of combining on-line feature selection with object tracking. For mpeg videos of these examples, please see <http://www.cs.cmu.edu/~rcollins/Pub/iccv03.html>.

The first video is low-contrast aerial footage of a car driving through patches of sunlight and shadow. Watching the video frame-by-frame, it is challenging even for a human observer to delineate the position of the car when it passes through shadow regions. Despite the difficulties, the tracker presented here smoothly tracks the car through the changing illumination conditions, and through partial occlusion caused by trees lining the road. Figure 6 presents a trace showing which 5 features out of 49 were chosen as most discriminative for each frame of the tracked sequence. We see that many of the same features are selected through most of the video (horizontal bars in the picture represent the same features being chosen again and again), and many features were never selected (empty rows). At a coarse level of description, the feature history can be broken into five blocks of frames, where roughly the same set of features were chosen consistently within each block, and the discontinuity between blocks is marked by a switch to a different set of features. Figure 6 also shows representative frames from within each of these five coarsely segmented time blocks. For the first, middle and last block, the car is predominantly

driving through sunny road or dappled patches of shadow. The second block delineates a subsequence where the car plunges into an area of deep, extended shadow. The fourth block denotes a subsequence where the car travels over a small bridge that has color properties similar to the car.

Figure 7A illustrates failure of a standard mean-shift tracker [4] on this section of the video. Standard mean-shift tracking is based only on an appearance model of the object. When the car passes over a small bridge, the color of the top of the bridge rail is nearly identical to the color of the specular highlight on top of the car. The mean-shift tracker gets sidetracked by this similar color, leading to tracking failure. Figure 7B shows the results of our adaptive tracker. Because this tracker maintains a model of both object AND background color distributions, it detects that a color in the background is similar to a color in the model, and automatically down-weights those pixels. The tracker is therefore not attracted to the bridge railing, and tracking proceeds.

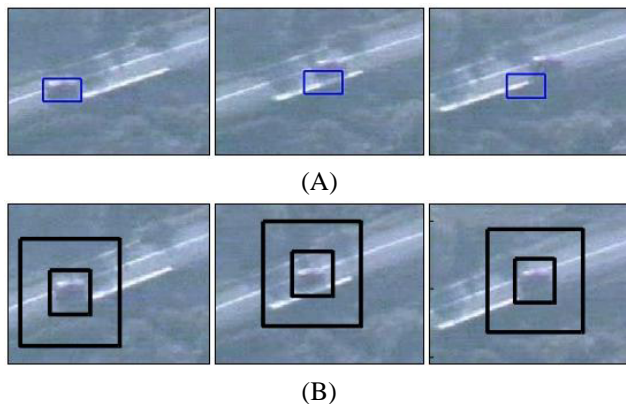


Figure 7: (A) The traditional mean-shift tracker is attracted to background pixels that have the same color as part of the tracked car, leading to tracking failure. (B) By modeling both object AND background color distributions, our tracking approach automatically down-weights shared colors, thus avoiding temptation.

A second example video is depicted in Figure 8. The object being tracked is a flag, blowing non-rigidly in the wind. The camera viewpoint continually changes, causing the scene background to vary. The flag is sometimes seen as a bright object against dark trees, and sometimes seen as a darker object backlit by the bright sky. Nonetheless, the tracker successfully follows the flag through the entire minute-long sequence. Figure 8 presents a trace showing which 5 features out of 49 were chosen as most discriminative for each frame of the tracked sequence. Again we see that many of the same features are selected through most of the video. However, we also note that these are different features than the ones chosen in the earlier car tracking example. There is a lot of variation in background clutter and illumination conditions throughout this sequence, and

coarsely segmenting the feature selection trace into time blocks, as we did in the earlier example, is difficult. Instead, we show a few sample frames from the tracked sequence, with an indication of where they occur.

## 5. Summary

Although object tracking based on color histogram appearance models can achieve real-time tracking performance, tracking success or failure depends primarily on how distinguishable the object is from its surroundings. Surprisingly, most tracking applications are conducted using a fixed feature space, determined a priori. These approaches ignore the fact that it is the ability to distinguish between object and background that is most important, and that the appearance of both the object and the background will change as the target object moves from place to place.

This paper presents an effective method for continuously evaluating multiple feature spaces while tracking, and for adjusting the set of features used to improve tracking performance. We develop an on-line feature ranking mechanism based on the two-class variance ratio measure, applied to log likelihood distributions computed with respect to a given feature from samples of object and background pixels. This feature ranking mechanism is embedded in a tracking system that adaptively selects the top-ranked features for tracking. The result is a system in which the features used for tracking and the appearance models of object and background co-evolve over time. The experimental results demonstrate successful tracking performance even on challenging video sequences.

Although the variance ratio is a computationally efficient mechanism for selecting features, it does not take into account the spatial distribution of values in the likelihood image. A good likelihood image for tracking should contain a blob of high likelihood values (centered on the object), surrounded by a ring of low likelihood values, to ensure that the tracker does not get misled. Our future work will focus on methods that ensure this spatial consistency, while still being computationally efficient.

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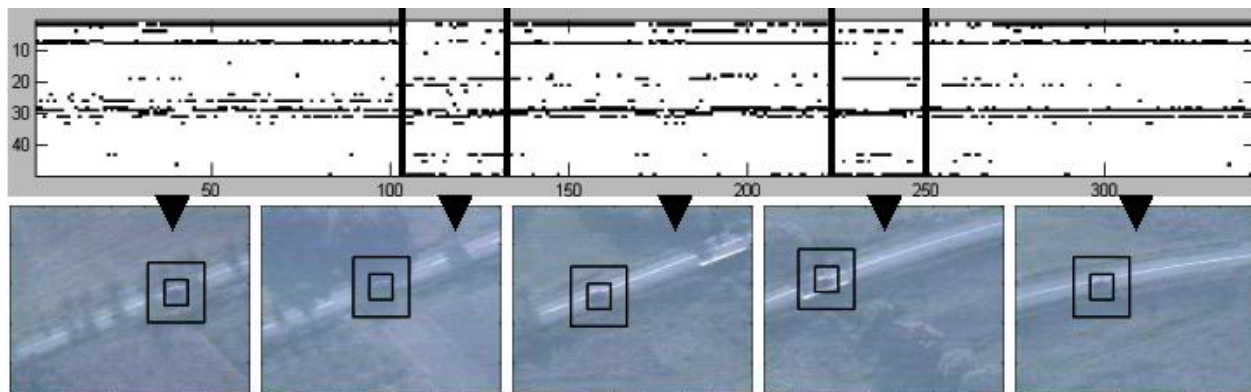


Figure 6: Trace of features selected to track a car through a hazy aerial video sequence. The car is successfully tracked through shadows and partial occlusion by trees lining the road. See text for details.

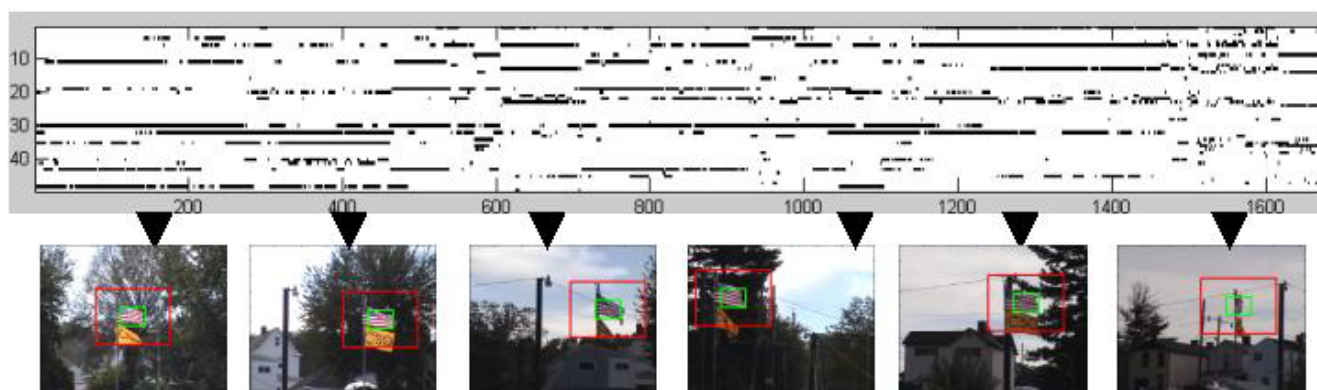


Figure 8: Trace of selected features over a one-minute long tracking sequence. The object tracked is a flag waving non-rigidly in the breeze. The camera motion leads to a wide range of changing background and illumination conditions, all of which are handled successfully by the tracker.

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