# CS4442/9542b: Artificial Intelligence II Prof. Olga Veksler

Lecture 16: Computer Vision Motion

Slides are from Steve Seitz (UW), David Jacobs (UMD)



# Why estimate motion?

- Lots of uses
  - Track object(s)
  - Correct for camera jitter (stabilization)
  - Align images (mosaics)
  - 3D shape reconstruction
  - Special effects



# **Optical Flow and Motion Field**

- Optical flow is the apparent motion of brightness patterns between 2 (or several) frames in an image sequence
- Why does brightness change between frames?
- Assuming that illumination does not change:
  - changes are due to the RELATIVE MOTION between the scene and the camera
  - There are 3 possibilities:
    - Camera still, moving scene
    - Moving camera, still scene
    - Moving camera, moving scene
- Optical Flow is what we *can* estimate from image sequences

















$$\frac{Computing Optical Flow: Brightness Constancy Equation}{I[x(t),y(t),t] = constant}$$

$$I[x(t),y(t),t] = constant$$
Taking derivative with respect to time:  

$$\frac{d I[x(t),y(t),t]}{dt} = 0$$

$$\bigcup_{\substack{i \in I \\ \partial x \ \partial t}} \frac{\partial I}{\partial x} \frac{\partial x}{\partial t} + \frac{\partial I}{\partial y} \frac{\partial y}{\partial t} + \frac{\partial I}{\partial t} = 0$$





























### **Observation**

- This is a two image problem BUT
  - Can measure sensitivity by just looking at one of the images!
  - This tells us which pixels are easy to track, which are hard
    - very useful for feature tracking

## Errors in Lucas-Kanade

- What are the potential causes of errors in this procedure?
  - Suppose A<sup>T</sup>A is easily invertible
  - Suppose there is not much noise in the image
- When our assumptions are violated
  - Brightness constancy is not satisfied
  - The motion is not small
  - A point does **not** move like its neighbors
    - window size is too large
    - what is the ideal window size?

# **Iterative Refinement**

- Iterative Lucas-Kanade Algorithm
  - 1. Estimate velocity at each pixel by solving Lucas-Kanade equations
  - 2. Warp H towards I using the estimated flow field use image warping techniques
  - 3. Repeat until convergence







![](_page_17_Figure_0.jpeg)

![](_page_17_Figure_1.jpeg)

![](_page_18_Figure_0.jpeg)

![](_page_18_Figure_1.jpeg)

![](_page_19_Figure_0.jpeg)

![](_page_19_Figure_1.jpeg)

![](_page_20_Figure_0.jpeg)

![](_page_20_Figure_1.jpeg)

### Tracking features

- Feature tracking
  - Compute optical flow for that feature for each consecutive H, I
- When will this go wrong?
  - Occlusions—feature may disappear
    - need mechanism for deleting, adding new features
  - Changes in shape, orientation
    - allow the feature to deform
  - Changes in color
  - Large motions
    - will pyramid techniques work for feature tracking?

#### Tracking Over Many Frames

- Feature tracking with m frames
  - 1. Select features in first frame
  - 2. Given feature in frame i, compute position in i+1
  - 3. Select more features if needed
  - **4**. i = i + 1
  - 5. If i < m, go to step 2

#### Issues

- Discrete search vs. Lucas Kanade?
  - depends on expected magnitude of motion
  - discrete search is more flexible
- Compare feature in frame i to i+1 or frame 1 to i+1?
  - affects tendency to drift..
  - How big should search window be?
    - too small: lost features. Too large: slow