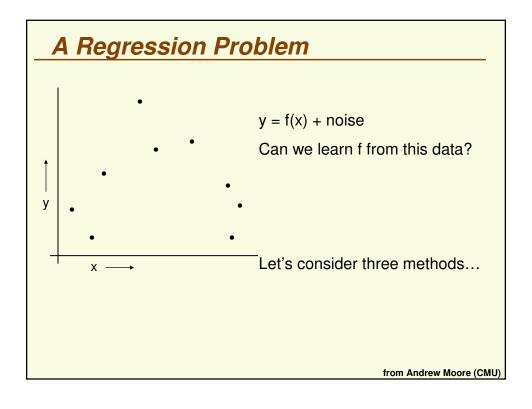
CS4442/9542b: Artificial Intelligence II Prof. Olga Veksler

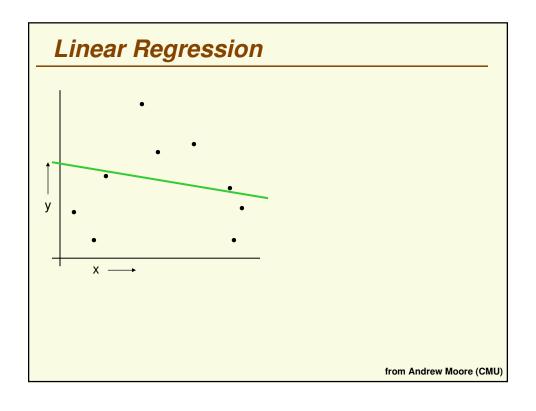
Lecture 7

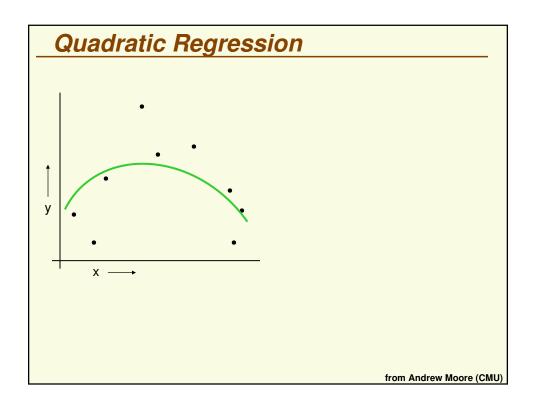
Machine Learning: Cross Validation

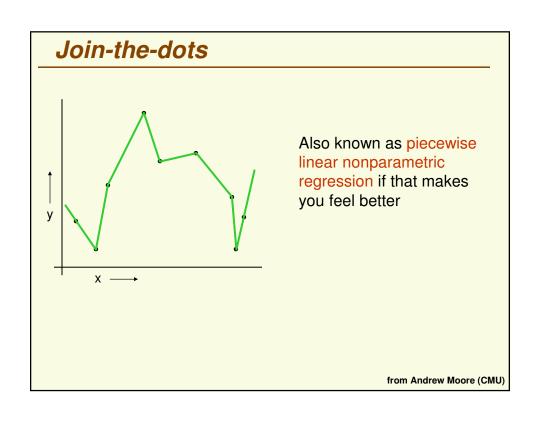
Outline

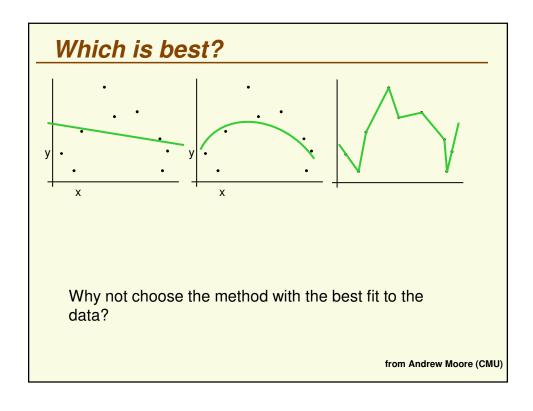
- Performance evaluation methods
 - test/train sets
 - cross-validation
 - k-fold
 - Leave-one-out

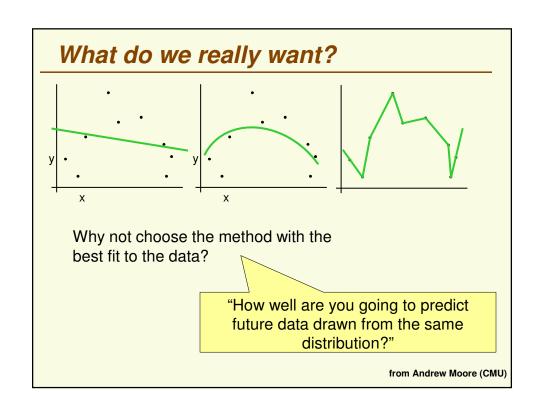


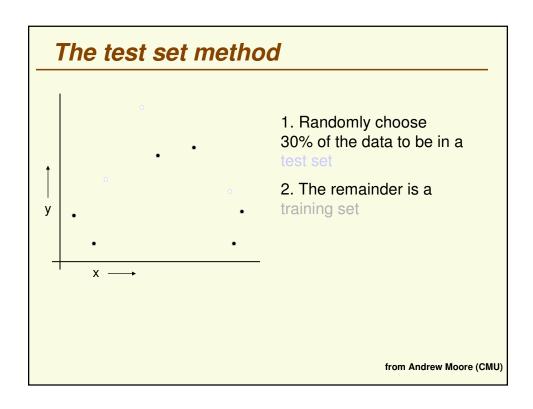


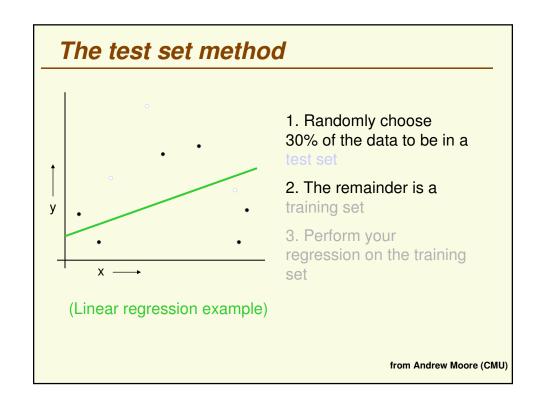




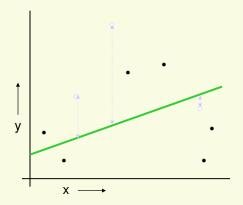












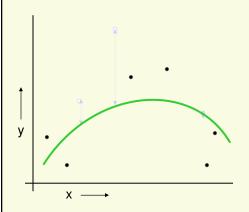
(Linear regression example)

Mean Squared Error = 2.4

- 1. Randomly choose 30% of the data to be in a test set
- 2. The remainder is a training set
- 3. Perform your regression on the training set
- Estimate your future performance with the test set

from Andrew Moore (CMU)

The test set method

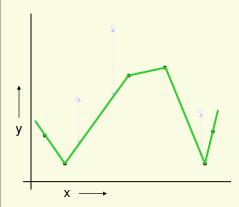


(Quadratic regression example)

Mean Squared Error = 0.9

- 1. Randomly choose 30% of the data to be in a test set
- 2. The remainder is a training set
- 3. Perform your regression on the training set
- 4. Estimate your future performance with the test set

The test set method



(Join the dots example)

Mean Squared Error = 2.2

- 1. Randomly choose 30% of the data to be in a test set
- 2. The remainder is a training set
- 3. Perform your regression on the training set
- Estimate your future performance with the test set

from Andrew Moore (CMU)

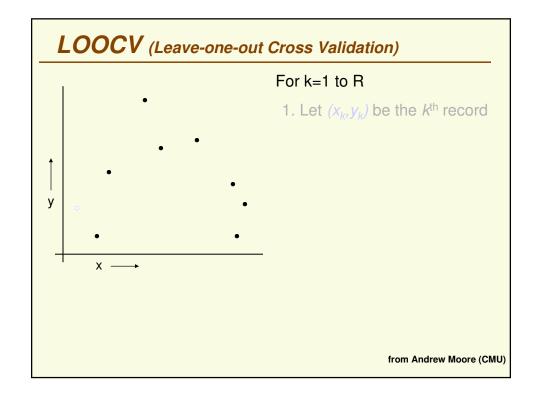
The test set method

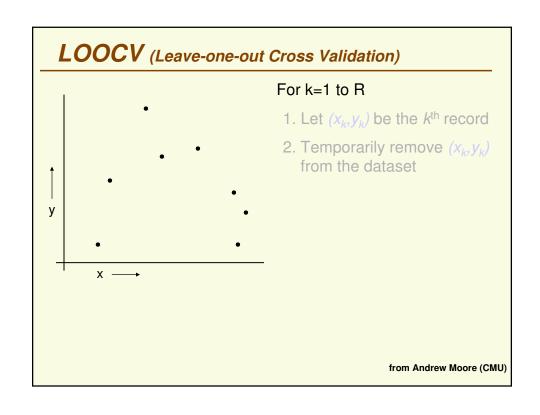
- Good news:
- Very very simple
- Can then simply choose the method with the best test-set score
- Bad news:
- What's the downside?

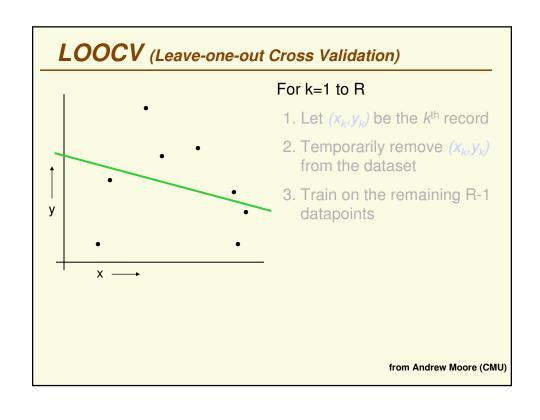
The test set method

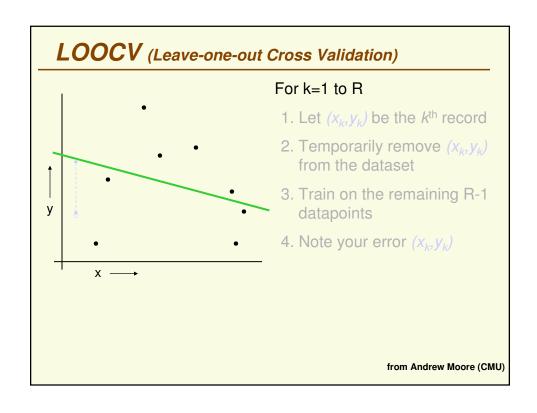
- Good news:
- ■Very very simple
- Can then simply choose the method with the best test-set score
- ■Bad news:
- ■Wastes data: we get an estimate of the best method to apply to 30% less data
 - •if we don't have much data, our testset might just be lucky or unlucky

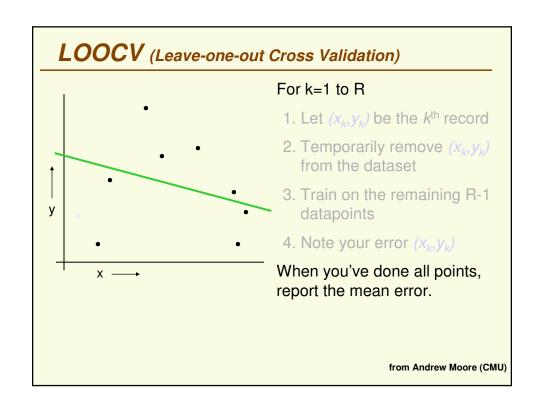
We say the "test-set estimator of performance has high variance"

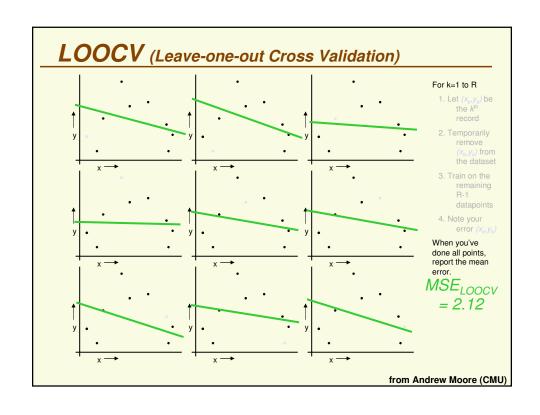


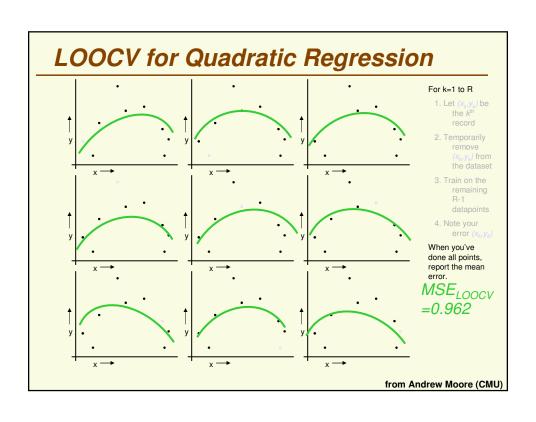


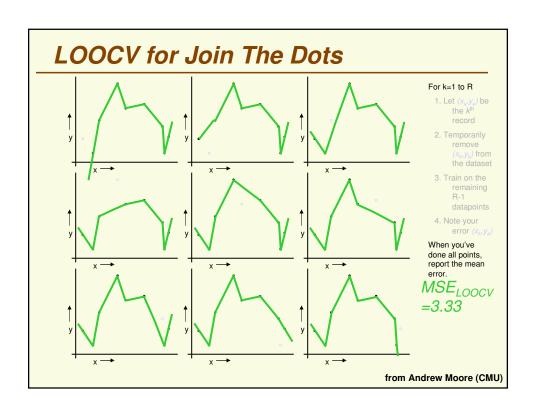








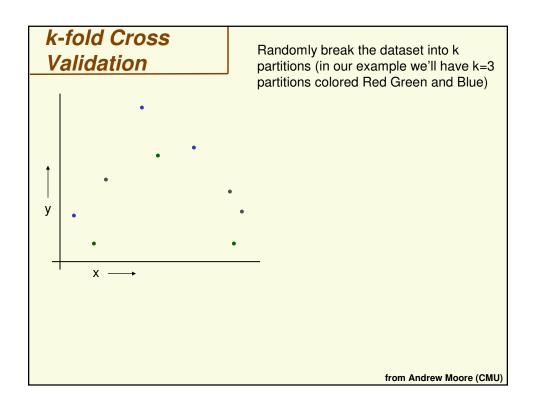


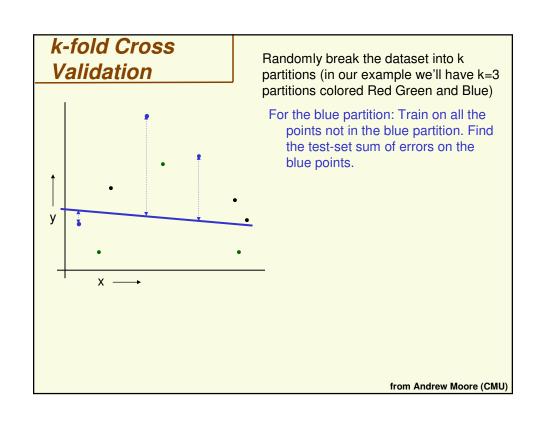


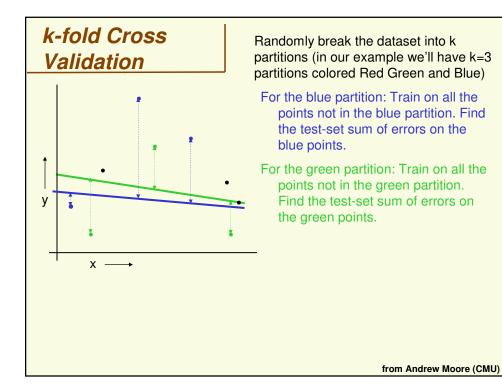
Which kind of Cross Validation?

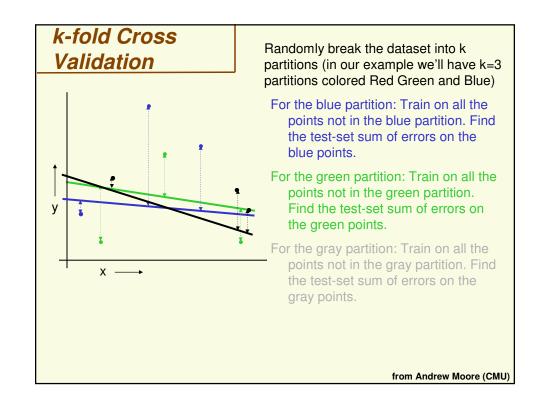
	Downside	Upside
Test-set	Variance: unreliable estimate of future performance	Cheap
Leave- one-out	Expensive	Doesn't waste data

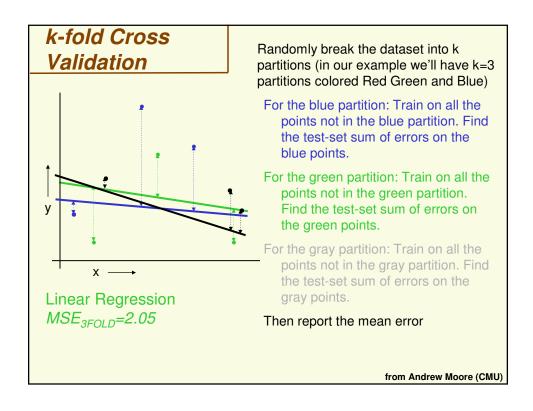
..can we get the best of both worlds?

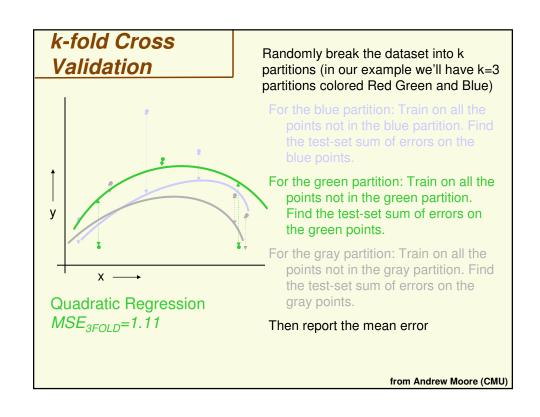


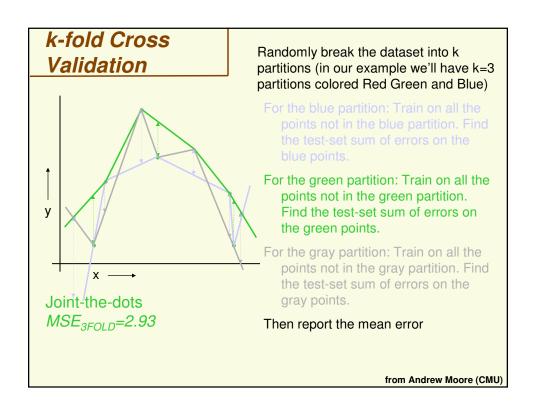












Which kind of Cross Validation?			
	Downside	Upside	
Test-set	Variance: unreliable estimate of future performance	Cheap	
Leave- one-out	Expensive	Doesn't waste data	
10-fold	Wastes 10% of the data. 10 times more expensive than test set	Only wastes 10%. Only 10 times more expensive instead of R times.	
3-fold	Wastier than 10-fold. Expensivier than test set	Slightly better than test- set	
N-fold	Identical to Leave-one-out		
		from Andrew Moore (CMU)	

CV-based Model Selection

- We're trying to decide which algorithm to use.
- We train each machine and make a table...

i	f_{i}	TRAINERR	10-FOLD-CV-ERR	Choice
1	f_1			
2	f_2			
3	f_3			√
4	f_4			
5	f_5			
6	f_6	I		

from Andrew Moore (CMU)

CV-based Model Selection

- Example: Choosing number of hidden units in a onehidden-layer neural net.
- Step 1: Compute 10-fold CV error for six different model

Algorithm	TRAINERR	10-FOLD-CV-ERR	Choice
0 hidden units			
1 hidden units			
2 hidden units			√
3 hidden units			
4 hidden units			
5 hidden units			

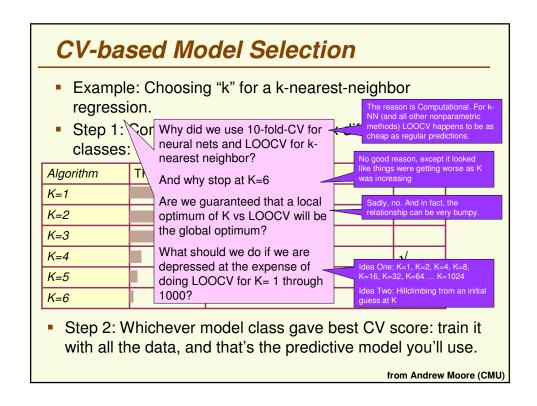
 Step 2: Whichever model class gave best CV score: train it with all the data, and that's the predictive model you'll use.

CV-based Model Selection

- Example: Choosing "k" for a k-nearest-neighbor regression.
- Step 1: Compute LOOCV error for six different model classes:

Algorithm	TRAINERR	10-fold-CV-ERR	Choice
K=1			
K=2			
K=3			
K=4			√
K=5			
K=6			

 Step 2: Whichever model class gave best CV score: train it with all the data, and that's the predictive model you'll use.



CV-based Algorithm Choice

- Example: Choosing which regression algorithm to use
- Step 1: Compute 10-fold-CV error for six different model classes:

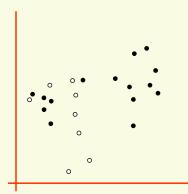
Algorithm	TRAINERR	10-fold-CV-ERR	Choice
1-NN			
10-NN			
Linear Reg'n			
Quad reg'n			√
LWR, KW=0.1			
LWR, KW=0.5			

 Step 2: Whichever algorithm gave best CV score: train it with all the data, and that's the predictive model you'll use.

from Andrew Moore (CMU)

Cross-validation for classification

- Instead of computing the sum squared errors on a test set, you should compute...
 - The total number of misclassifications on a testset



- What's LOOCV of 1-NN?
- What's LOOCV of 3-NN?
- What's LOOCV of 22-NN?