CS4442/9542b Artificial Intelligence II prof. Olga Veksler

> Lecture 11 Computer Vision Stereo

> > Some slides are from S. Seitz, S. Narasimhan, K. Grauman

Outline

- Cues for 3D reconstruction
- Stereo Cues
- Stereo Reconstruction
 - 1) camera calibration and rectification
 - an easier, mostly solved problem
 - 2) stereo correspondence
 - a harder problem

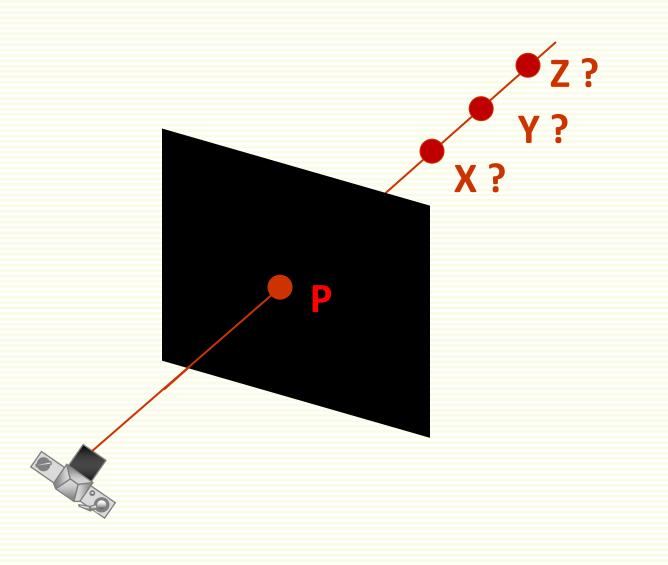
2D Images

- World is 3D
- In 2D images, depth (the third coordinate) is largely lost
 - includes human retina



2D Images

• Depth is inherently ambiguous from a single view



Street Pavement Art

• Viewed from the "right" side



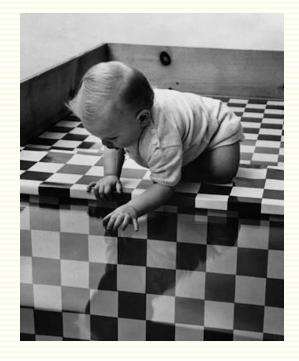
Street Pavement Art

• Viewed from the "wrong" side



Babies and Animals Perceive Depth

• Yet we perceive the world in 3D





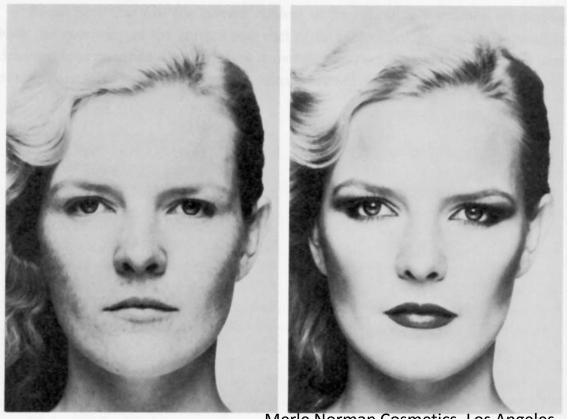
The Visual Cliff, by William Vandivert, 1960

3D Shape from Images

- What image cues provide 3D information?
- Cues from a single image
- Cues from multiple images
 - Motion cues
 - Stereo cues
- Can we use these cues in a computer vision system?

Single Image 3D Cues: Shading

• Pixels covered by shadow are perceived to be further away



Merle Norman Cosmetics, Los Angeles

Single Image 3D Cues: Linear Perspective

• The further away are parallel lines, the closer they come together



Single Image 3D Cues: Relative Size

• If objects have the same size, those further away appear smaller



Single Image 3D Cues: Texture

• Further away texture appears finer (smaller scale)

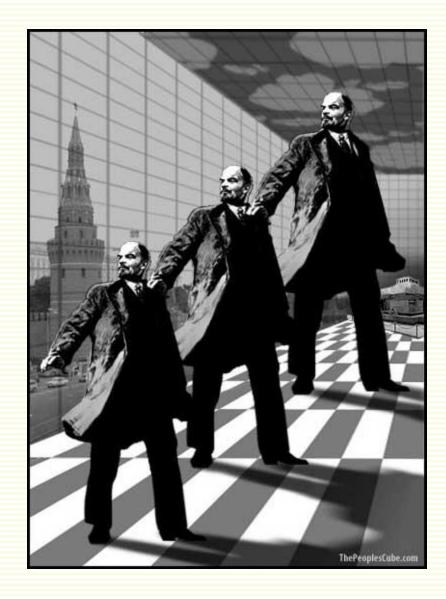


Single Image 3D Cues: Known Size

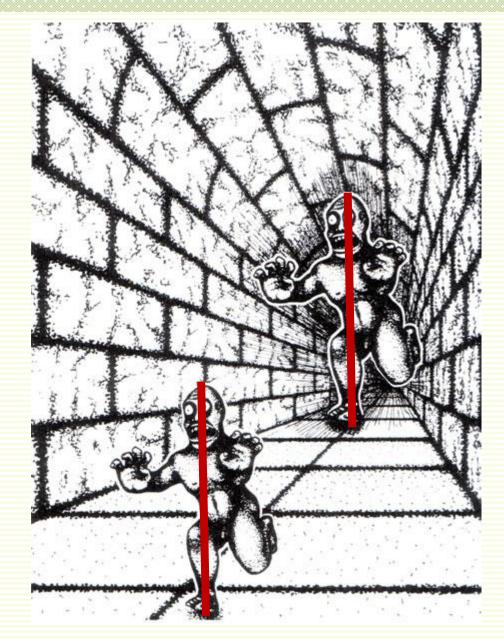
• Ducks are smaller than elephants, duck is closer



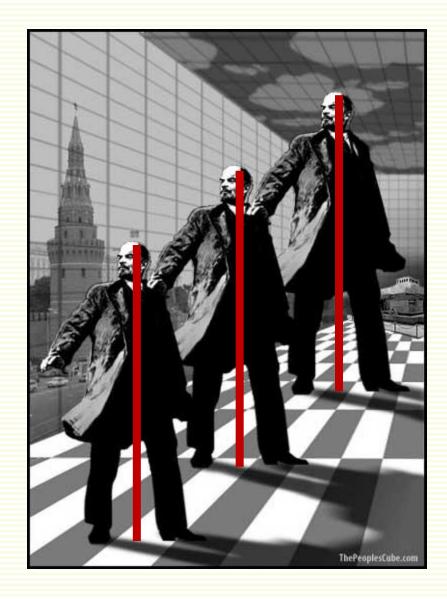
Illusions: Linear Perspective + Relative Size



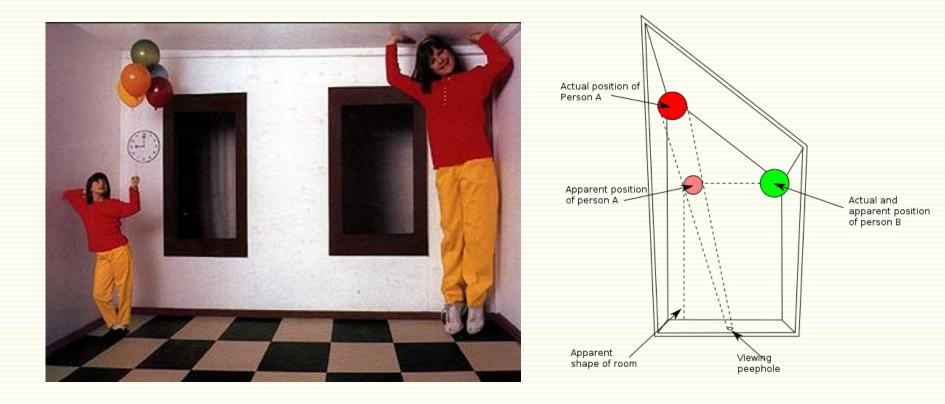
Illusions: Linear Perspective + Relative Size



Illusions: Linear Perspective + Relative Size

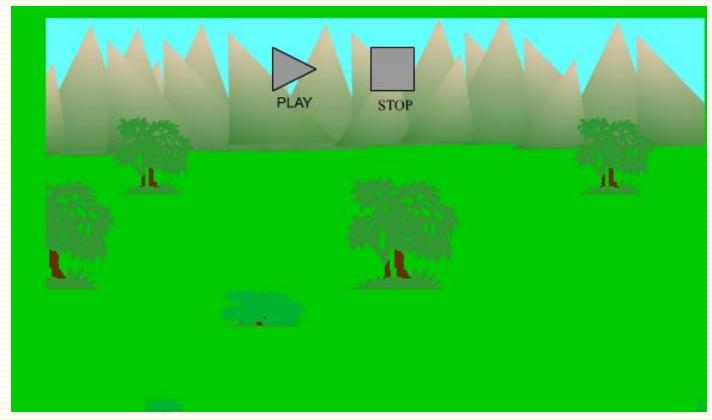


Illusions: Ames Room



Cues from Multiple Image: Motion Parallax

• Closer objects appear to move more than further away objects



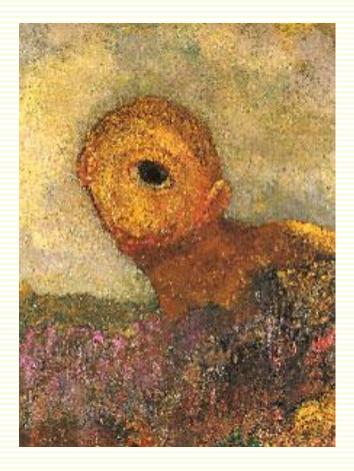
http://psych.hanover.edu/KRANTZ/MotionParallax/MotionParallax.html

3D Shape from X

- **X** = shading, texture, motion, ...
- We will focus on **stereo**
 - depth perception from two stereo images

Why Two Eyes? Cylopes?

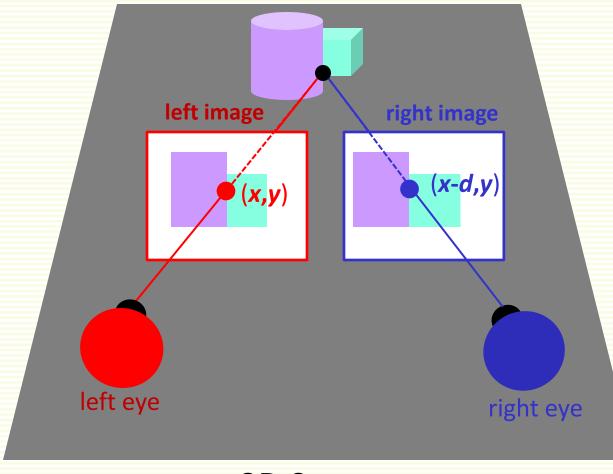




Why Two Eyes?

• Charles Wheatstone first explained stereopsis in 1838

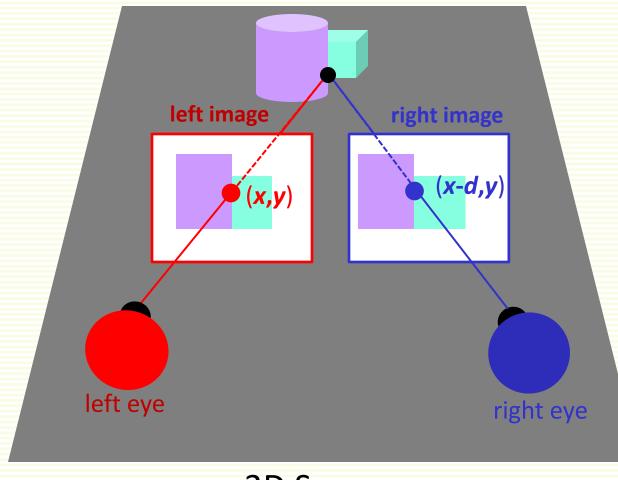




3D Scene

Why Two Eyes?

• **Disparity** *d* is the difference in **x** coordinates of corresponding points



3D Scene



• Wheatstone invented the first stereoscope





Anaglyph Images

- Encodes left and right image into a single picture
 - left eye image is transferred to the red channel
 - right eye image to the green+blue = cyan channel
- Red filter lets through only the left image
- Cyan filter lets through only theright eye image
- Brain fuses into 3D
- Similar technology for 3D movies
- Works for most of us

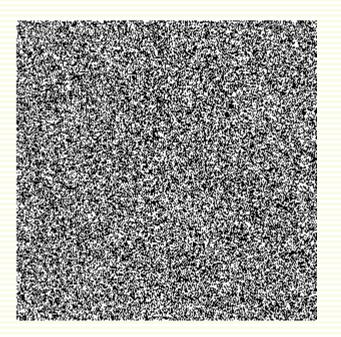




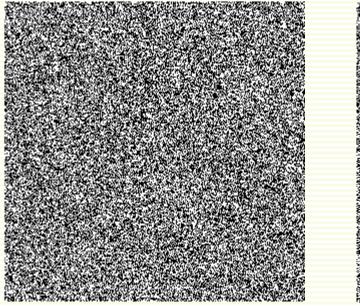


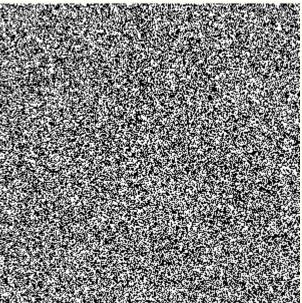
What is Needed for Stereopsis?

- Need monocular cues for stereopsis? Need object cues? Answered by Julesz in 1960
- Image with no monocular cues and no recognizable objects: random dots

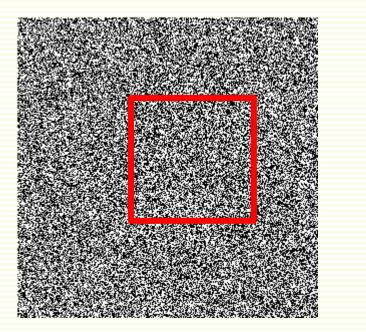


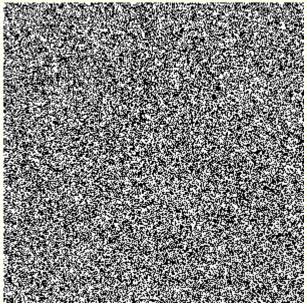
- Answered by Julesz in 1960
- Make a copy of it



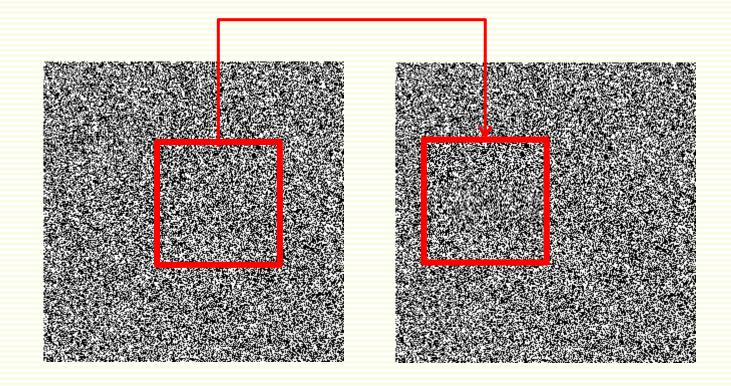


- Answered by Julesz in 1960
- Select a square

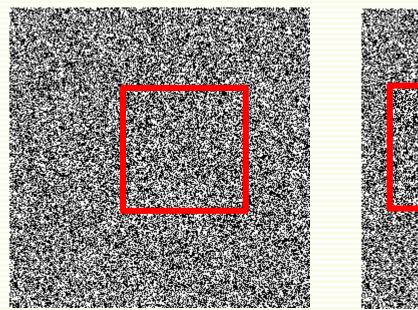


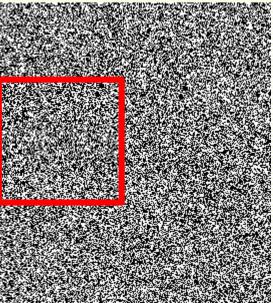


- Answered by Julesz in 1960
- Copy square the right image, shifting by d to the left
 - random dot stereogram



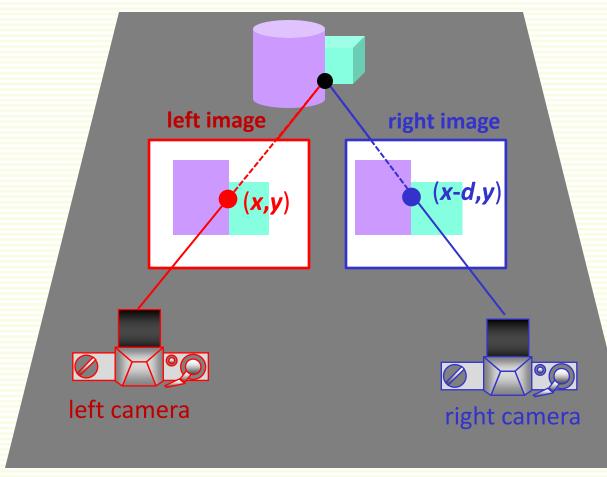
- Answered by Julesz in 1960
- Random dot stereogram
- Humans perceive square floating in front of background





3D Shape from Stereo

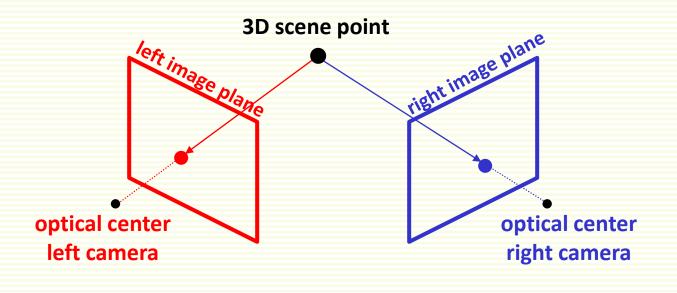
• Use two cameras instead of two eyes



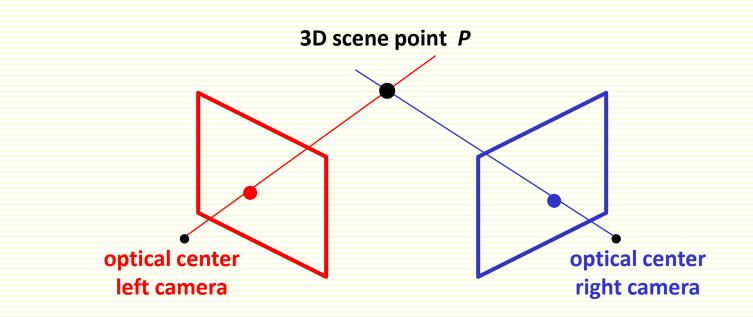
3D Scene

Stereo System

- Unlike eyes, usually stereo cameras are not on the same plane
 - better numerical stability



Stereo System: Triangulation



- Depth by triangulation
 - given two corresponding points in the left and right image
 - cast the rays through the optical camera centers
 - ray intersection is the corresponding 3D world point **P**
 - depth of **P** is based on camera positions and parameters
- Triangulation ideas can be traced to ancient Greece



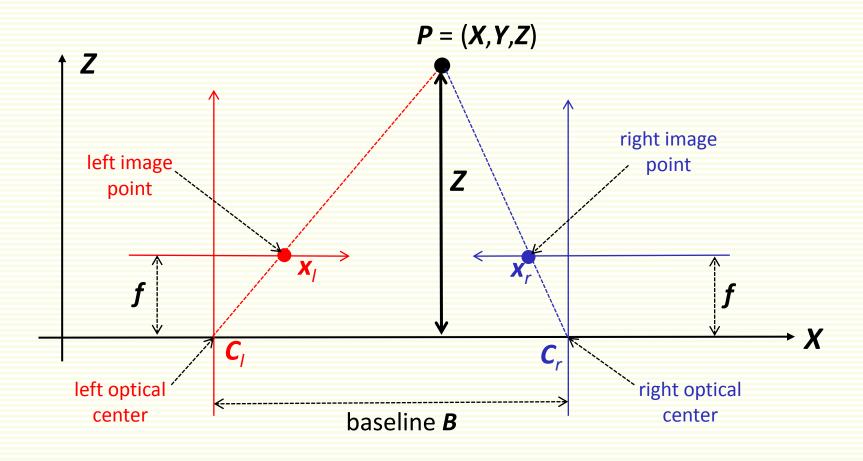
document from 1533

What is needed for Triangulation

- 1. Distance between cameras, camera focal length
 - Solved through camera calibration, essentially a solved problem
 - We will not talk about it
 - Code available on the web
 - OpenCV <u>http://www.intel.com/research/mrl/research/opencv/</u>
 - Matlab, J. Bouget http://www.vision.caltech.edu/bouguetj/calib_doc/index.html
 - Zhengyou Zhang http://research.microsoft.com/~zhang/Calib/
- 2. Pairs of corresponding pixels in left and right images
 - Called stereo correspondence problem, still much researched

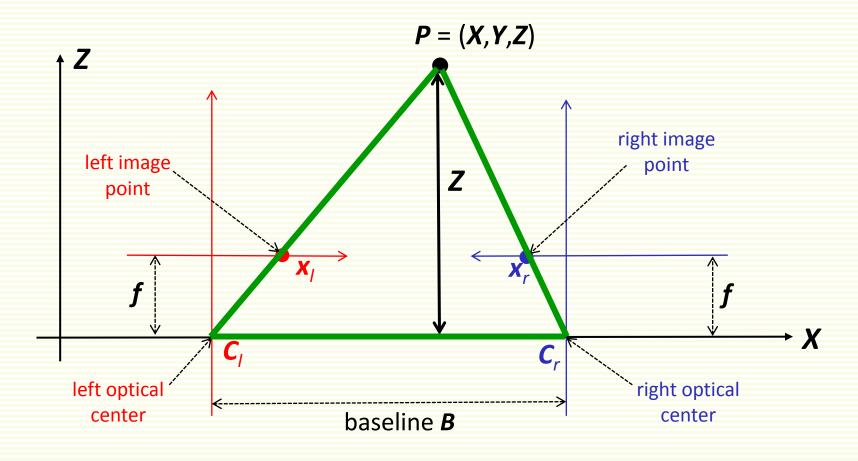
Formula: Depth from Disparity

- Top down view on geometry (slice through *XZ* plane)
 - from camera calibration, know the distance between camera optical centers called **baseline** *B*, and camera focal length *f*



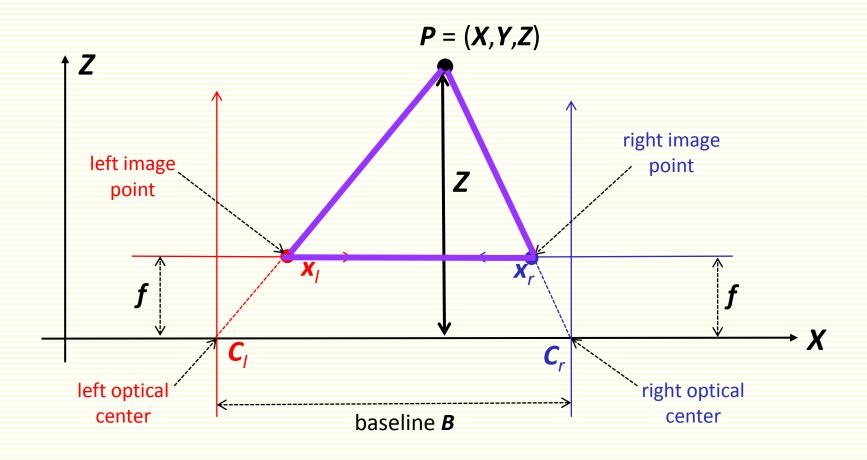
Formula: Depth from Disparity

• Height to base ratio of triangle $C_{\rm I} P C_{\rm r}$: $\frac{Z}{B}$



Formula: Depth from Disparity

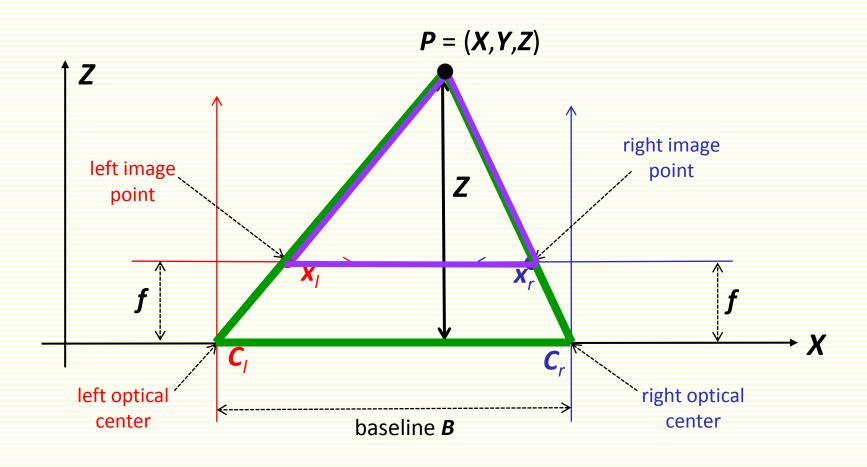
- Height to base ratio of triangle $x_{l}Px_{r}$: $\frac{Z-f}{B-x_{l}+x_{r}}$
- **x**₁ is positive, **x**_r is negative



Formula: Depth from Disparity

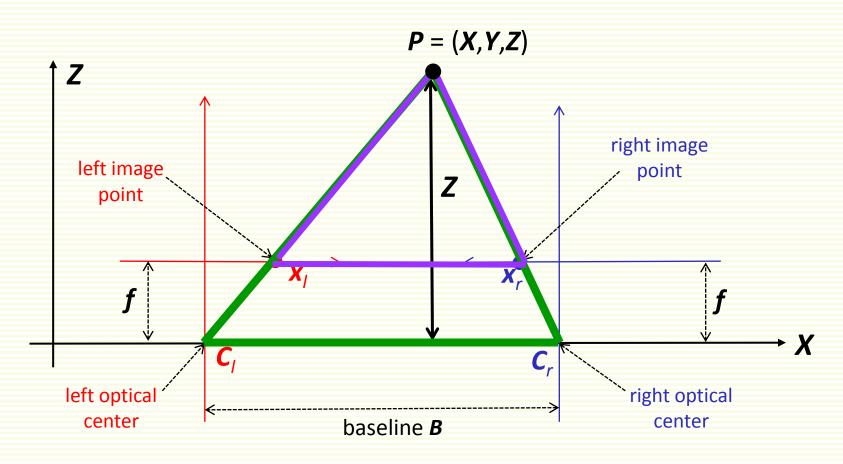
• $C_{|}PC_{r}$ and $\Delta x_{|}P x_{r}$ are similar:

 $\frac{Z}{B} = \frac{Z - f}{B - x_1 + x_r}$



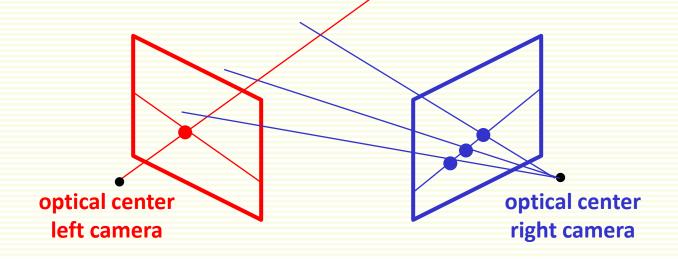
Formula: Depth from Disparity

- Rewriting: $Z = \frac{B \cdot f}{x_l x_r}$
- **x**₁ **x**_r is the **disparity**



Stereo Correspondence: Epipolar Lines

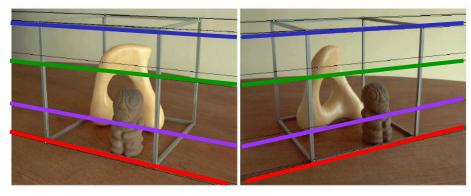
• Which pairs of pixels correspond to the same scene element ?



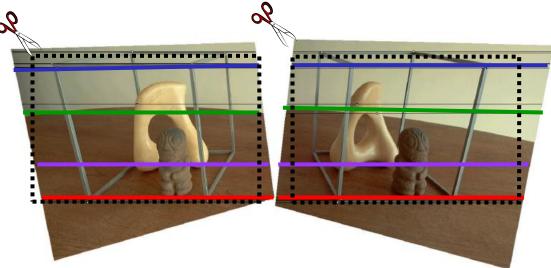
- Epipolar constraint
 - Given a left image pixel, the corresponding pixel in the right image must lie on a line called the **epipolar** line
 - reduces correspondence to 1D search along **conjugate** epipolar lines
 - demo: <u>http://www.ai.sri.com/~luong/research/Meta3DViewer/EpipolarGeo.html</u>

Stereo Rectification

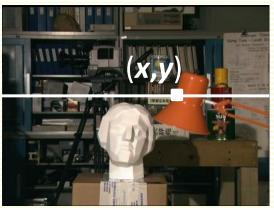
• Epipolar lines can be computed from camera calibration



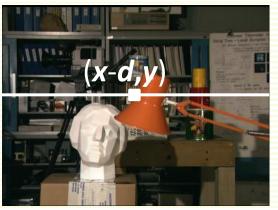
- Usually they are not horizontal
- Can **rectify** stereo pair to make epipolar lines horizontal



Stereo Correspondence



left image

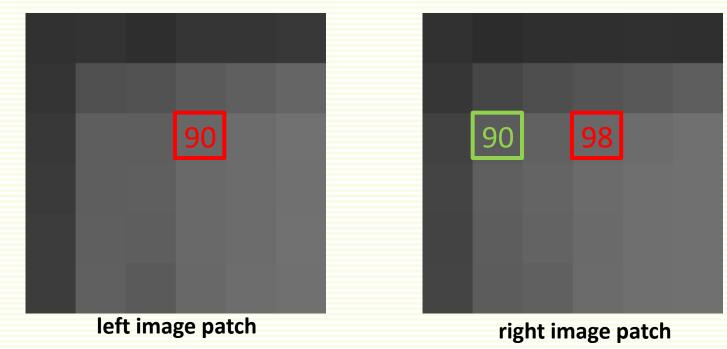


right image

- From now on assume stereo pair is rectified
- How to solve the correspondence problem?
- Corresponding pixels should be similar in intensity
 - or color, or something else

Difficulties in Stereo Correspondence

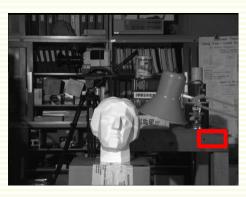
- Image noise
 - corresponding pixels have similar, but not exactly the same intensities



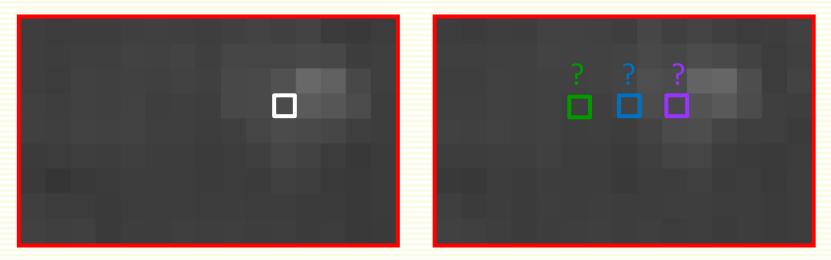
• Matching each pixel individually is unreliable

Difficulties in Stereo Correspondence

• regions with (almost) constant intensity

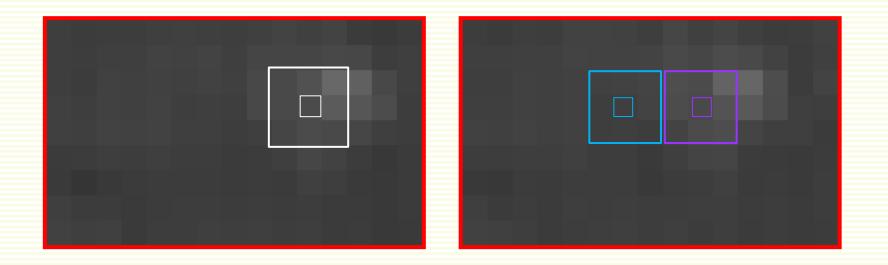






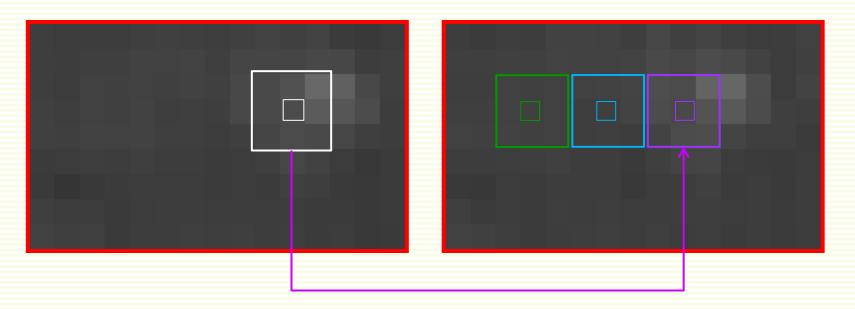
• Matching each pixel individually is unreliable

Window Matching Correspondence



- Use a window (patch) of pixels
 - more likely to have enough intensity variation to form a distinguishable pattern
 - also more robust to noise

Window Matching Correspondence



- Use a window (patch) of pixels
 - more likely to have enough intensity variation to form a distinguishable pattern
 - also more robust to noise

Window Matching: Basic Algorithm



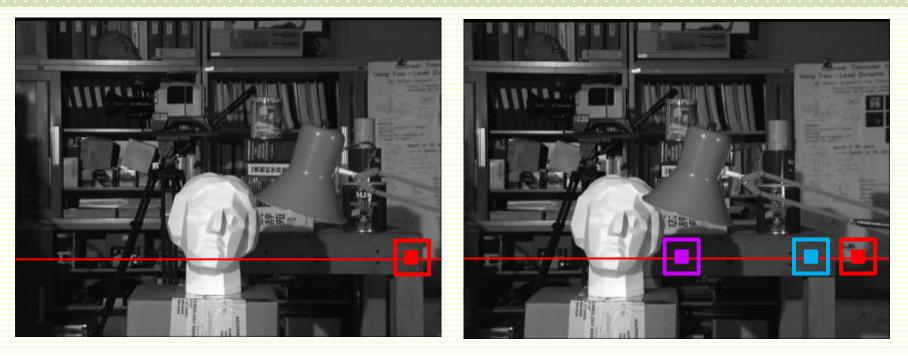
- for each epipolar line
 - for each pixel **p** on the left line
 - compare window around *p* with same window shifted to many right window locations on corresponding epipolar line
 - pick location corresponding to the best matching window

Which Locations to Try?



- Disparity cannot be negative
- Maximum possible disparity is limited by the camera setup
 - assume we know maxDisp
- Disparity can range from **0** to **maxDisp**
 - consider only (*x*,*y*), (*x*-1,*y*),...(*x*-*maxDisp*,*y*) in the right image

Window Matching Cost



- How to define the best matching window?
- Define window cost
 - sum of squared differences (SSD)
 - or sum of absolute differences (SAD)
 - many other possibilities
- Pick window of best (smallest) cost

SSD Window Cost

left image

right image

			0-		
5	4	4	2	4	2
4	1	4	4	2	6
7	46	46	46	6	7
9	46	46	44	9	7
7	47	47	47	2	4
7	56	56	46	6	7
4	4	1	4	3	2
	4 7 9 7 7	 4 7 46 9 46 7 47 56 	5 4 4 4 1 4 7 46 46 9 46 46 7 47 47 7 56 56	5 4 4 2 4 1 4 4 7 46 46 46 9 46 46 44 7 47 47 47 7 56 56 46	5 4 4 2 4 4 1 4 4 2 7 46 46 46 6 9 46 46 44 9 7 47 47 47 2 7 56 56 46 6

		0		iu Sc		
з	5	4	4	2	4	2
7	4	1	4	4	2	6
46	46	46	3	6	6	7
48	46	44	6	4	9	7
47	47	47	7	4	2	4
58	56	46	5	6	6	7
3	4	4	1	4	3	2

 $(46-44)^{2} + (46-6)^{2} + (44-4)^{2} + (47-47)^{2} + (47-7)^{2} + (47-7)^{2} + (47-4)^{2} + (56-46)^{2} + (56-5)^{2} + (46-6)^{2} = 12454$

		left	ima	age			_			righ	it im	nage	Ņ
ß	5	4	4	2	4	2		3	5	4	4	2	
7	4	1	4	4	2	6		7	4	1	4	4	
2	7	46	46	46	6	7		46	46	46	3	6	
5	9	46	46	44	9	7		48	46	44	6	4	ſ
4	7	47	47	47	2	4		47	47	47	7	4	
4	7	56	56	46	6	7		58	56	46	5	6	
3	4	4	1	4	3	2		3	4	4	1	4	

 $(46-44)^{2} + (46-6)^{2} + (44-4)^{2} + (47-47)^{2} + (47-7)^{2} + (47-7)^{2} + (47-4)^{2} + (56-46)^{2} + (56-5)^{2} + (46-6)^{2} = 12454$

This shift corresponds to disparity 0

left image									
3	5	4	4	2	4	2			
7	4	1	4	4	2	6			
2	7	46	46	46	6	7			
5	9	46	46	44	9	7			
4	7	47	47	47	2	4			
4	7	56	56	46	6	7			
3	4	4	1	4	3	2			

3544242741442646464636674846446497474774245856465667			rigi	nt Im	lage		
46 46 46 3 6 6 7 48 46 44 6 4 9 7 47 47 47 7 4 2 4 58 56 46 5 6 6 7	3	5	4	4	2	4	2
48 46 44 6 4 9 7 47 47 47 7 4 2 4 58 56 46 5 6 6 7	7	4	1	4	4	2	6
47 47 47 7 4 2 4 58 56 46 5 6 6 7	46	46	46	3	6	6	7
58 56 46 5 6 6 7	48	46	44	6	4	9	7
	47	47	47	7	4	2	4
	58	56	46	5	6	6	7
3 4 4 1 4 3 2	3	4	4	1	4	3	2

right image

 $(46-46)^{2} + (46-44)^{2} + (44-6)^{2} + (47-47)^{2} + (47-7)^{2} + (47-7)^{2} + (47-7)^{2} + (56-56)^{2} + (56-46)^{2} + (46-5)^{2} = 6425$

• This shift corresponds to disparity 1

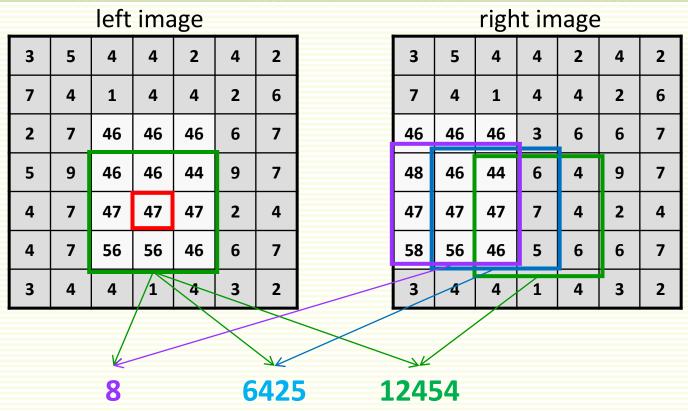
left image									
3	5	4	4	2	4	2			
7	4	1	4	4	2	6			
2	7	46	46	46	6	7			
5	9	46	46	44	9	7			
4	7	47	47	47	2	4			
4	7	56	56	46	6	7			
3	4	4	1	4	3	2			

			rigi		lage		
	3	5	4	4	2	4	2
	7	4	1	4	4	2	6
	46	46	46	3	6	6	7
	48	46	44	6	4	9	7
	47	47	47	7	4	2	4
	58	56	46	5	6	6	7
-	3	4	4	1	4	3	2

right imago

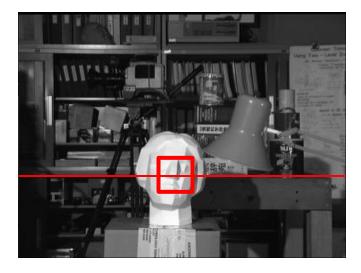
 $(46-48)^{2} + (46-46)^{2} + (44-44)^{2} + (47-47)^{2} + (47-47)^{2} + (47-47)^{2} + (56-58)^{2} + (56-56)^{2} + (46-46)^{2} = 8$

• This shift corresponds to disparity 2

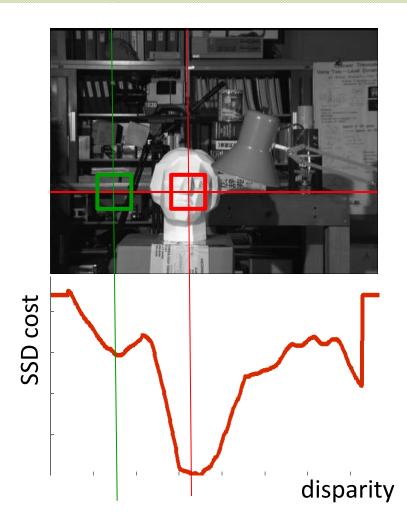


- Best SSD window cost is 8 at disparity 2
- Red pixel is assigned disparity 2
- Repeat this for all image pixels

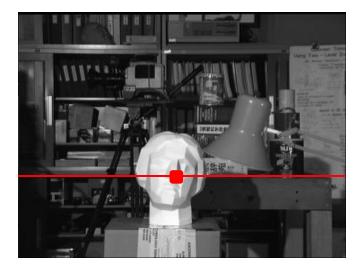
Correspondence with SSD Matching



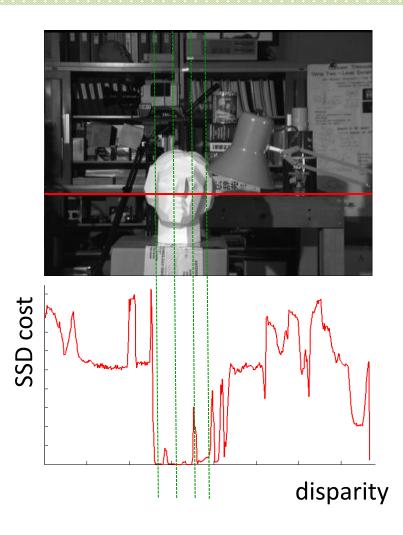
• Unique best cost location



Compare to One Pixel "Window"

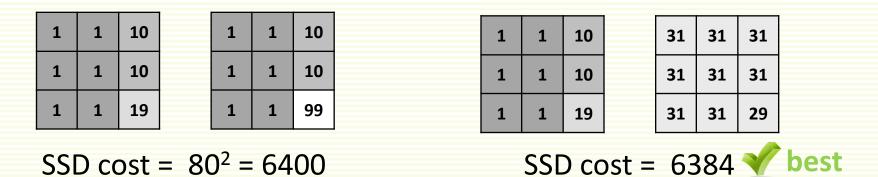


• No unique best cost location



SAD Window Cost

• SSD is fragile to outliers



• SAD (Sum of Absolute Differences) is more robust



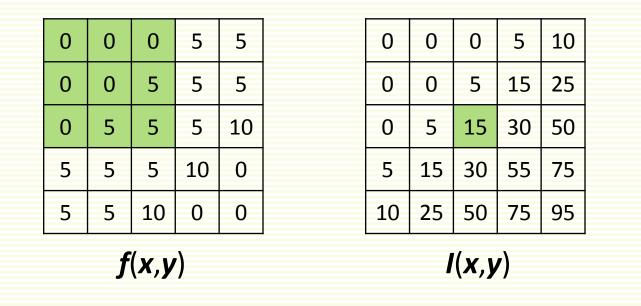
Window Matching Efficency

• Suppose

- image has *n* pixels
- matching window is **11** by **11**
- Need 11·11 = 121 additions and multiplications to compute one window cost
- Multiply that by number of locations to check (maxDisp+1)
- Multiply that by *n* image pixels
- **121** · *n* ·(maxDisp+1)
- Tooooo sloooow
 - gets worse for larger windows
- Can get cost down to *n* ·(maxDisp+1) with integral images

Speedups: Integral Image

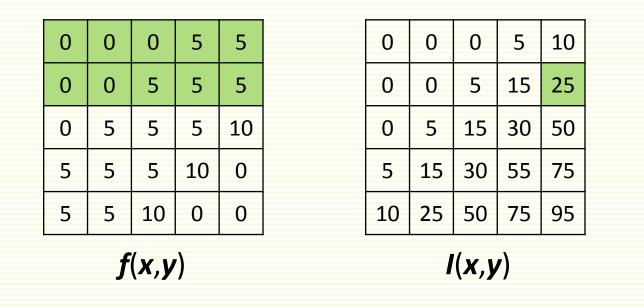
Given image f(x,y), the integral image l(x,y) is the sum of values in f(x,y) to the left and above (x,y), including (x,y)



• Example: *I*(2,2) = 0 + 0 + 0 + 0 + 0 + 5 + 0 + 5 + 5 = 15

Speedups: Integral Image

Given image f(x,y), the integral image l(x,y) is the sum of values in f(x,y) to the left and above (x,y), including (x,y)



• Example: *I*(4,1) = 0 + 0 + 0 + 5 + 5 + 0 + 0 + 5 + 5 = 25

• Suppose computed integral image up to location (*x*,*y*)

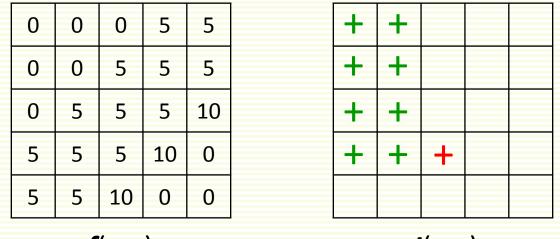
 $I(\boldsymbol{x},\boldsymbol{y}) = \boldsymbol{f}(\boldsymbol{x},\boldsymbol{y})$

0	0	0	5	5
0	0	5	5	5
0	5	5	5	10
5	5	5	10	0
5	5	10	0	0

f(x,y)

• Suppose computed integral image up to location (*x*,*y*)

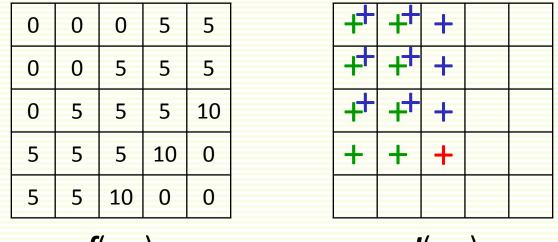
I(x,y) = f(x,y) + I(x-1,y)



f(*x*,*y*)

• Suppose computed integral image up to location (*x*,*y*)

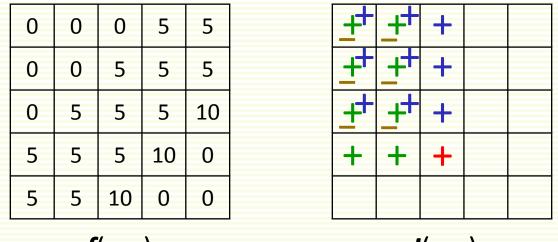
I(x,y) = f(x,y) + I(x-1,y) + I(x,y-1)



f(x,y)

• Suppose computed integral image up to location (x,y)

I(x,y) = f(x,y) + I(x-1,y) + I(x,y-1) - I(x-1,y-1)



f(*x*,*y*)

I(x,y)

Integral Image: Order of Computation

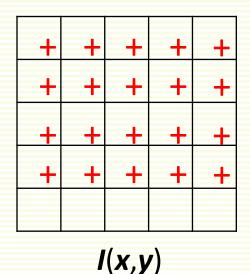
- Convenient order of computation
 - 1. first row
 - 2. first column
 - 3. the rest in row-wise fashion

2	3	4	5
10	11	12	13
14	15	16	17
18	19	20	21
22	23	24	25
	10 14 18	10 11 14 15 18 19	10 11 12 14 15 16 18 19 20

- After computed integral image, sum over any rectangular window is computed with four operations
- Top left corner $(\mathbf{x}_1, \mathbf{y}_1)$ and bottom right corner $(\mathbf{x}_2, \mathbf{y}_2)$

 $l(x_2, y_2)$

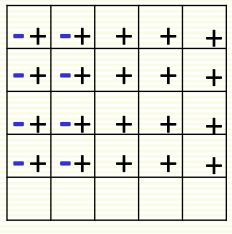
0	0	5	5	5
0	5	5	5	10
5	5	5 10	10 0	0
J	•	f(x , y		0



- After computed integral image, sum over any rectangular window is computed with four operations
- Top left corner $(\mathbf{x}_1, \mathbf{y}_1)$ and bottom right corner $(\mathbf{x}_2, \mathbf{y}_2)$

 $I(x_2, y_2) - I(x_1 - 1, y_2)$

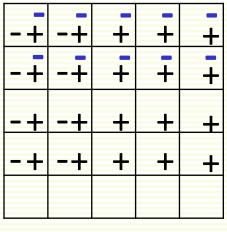
0 5 5 5				•
5 5 5 10	10 0	5	5	5



- After computed integral image, sum over any rectangular window is computed with four operations
- Top left corner $(\mathbf{x}_1, \mathbf{y}_1)$ and bottom right corner $(\mathbf{x}_2, \mathbf{y}_2)$

 $I(x_2,y_2) - I(x_1-1,y_2) - I(x_2,y_1-1)$

0	0	0	5	5
0	0	5	5	5
0	5	5	5	10
5	5	5	10	0
5	5	10	0	0
	f	f(x,y	/)	





- After computed integral image, sum over any rectangular window is computed with four operations
- Top left corner $(\mathbf{x}_1, \mathbf{y}_1)$ and bottom right corner $(\mathbf{x}_2, \mathbf{y}_2)$

 $I(x_2,y_2) - I(x_1-1,y_2) - I(x_2,y_1-1) + I(x_1-1,y_1-1)$

	0 0 0 5		5 5	5 5	5 10		
	5	5	5	10	0		
	5	5	10	0	0		
<i>f</i> (<i>x</i> , <i>y</i>)							

+ - - +	+- -+	- +	- +	- +
+- -+	+- +	-+	-+	-+
-+	-+	+	÷	+
-+	-+	+	Ŧ	+

- After computed integral image, sum over any rectangular window is computed with four operations
- Top left corner $(\mathbf{x}_1, \mathbf{y}_1)$ and bottom right corner $(\mathbf{x}_2, \mathbf{y}_2)$

 $I(x_2,y_2) - I(x_1-1,y_2) - I(x_2,y_1-1) + I(x_1-1,y_1-1)$

5

15

30

55

75 95

10

25

50

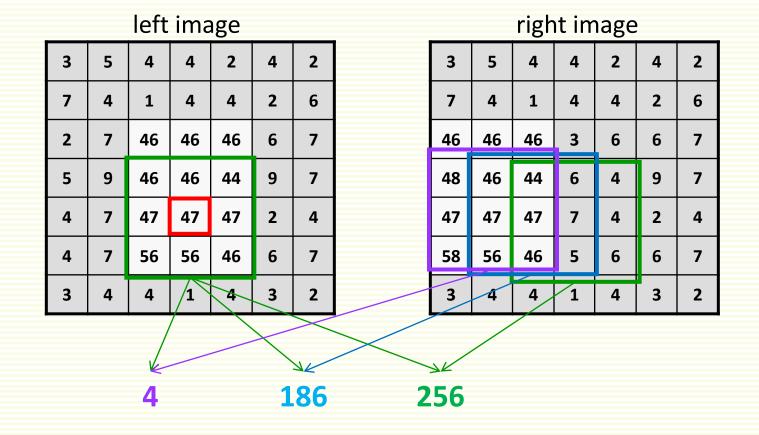
75

f(x,y)									
5	5	10	0	0		10	25	50	7
5	5	5	10	0		5	15	30	C)
0	5	5	5	10		0	5	15	(1)
0	0	5	5	5		0	0	5	1
0	0	0	5	5		0	0	0	

• Example: 5 + 5 + 10 + 5 + 10 + 0 = 75 - 15 - 25 + 0 = 35

Integral Image for Window Matching

- Assume SAD (sum of absolute differences) cost
- Need to find SAD for every pixel and every disparity in a window



Integral Image for Window Matching

- for each pixel **p**
 - for every disparity **d**
 - compute cost between window around *p* in the left image and the same window shifted by *d* in the right image
 - pick d corresponding to the best matching window

left image									
3	5	4	4	2	4	2			
7	4	1	4	4	2	6			
2	7	46	46	46	6	7			
5	9	46	46	44	9	7			
4	7	47	47	47	2	4			
4	7	56	56	46	6	7			
3	4	4	1	4	3	2			

right image

ingite intage									
3	5	4	4	2	4	2			
7	4	1	4	4	2	6			
46	46	46	3	6	6	7			
48	46	44	6	4	9	7			
47	47	47	7	4	2	4			
58	56	46	5	6	6	7			
3	4	4	1	4	3	2			

Integral Image for Window Matching

- For each disparity *d* need to compute window cost for all pixels, eventually
- For example, pick disparity **d** = 1

3	5	4	4	2	4	2		
7	4	1	4	4	2	6		
2	7	46	46	46	6	7		
5	9	46	46	44	9	7		
4	7	47	47	47	2	4		
4	7	56	56	46	6	7		
3	4	4	1	4	3	2		

left image

right image

- Old inefficient algorithm:
 - for each pixel *p* ←
 - for every disparity **d**
 - compute cost between window around *p* in the left image and the same window shifted by *d* in the right image

swap

- pick d corresponding to the best matching window
- New efficient algorithm:
 - for each disparity d
 - for every pixel **p**



- compute cost between window around *p* in the left image and the same window shifted by *d* in the right image
- pick **d** corresponding to the best matching window

• Suppose current disparity is **d** = 1

left image										
3	5	4	4	2	4	2				
7	4	1	4	4	2	6				
2	7	46	46	46	6	7				
5	9	46	46	44	9	7				
4	7	47	47	47	2	4				
4	7	56	56	46	6	7				
3	4	4	1	4	3	2				

right image

- Overlay left and right image at disparity 1
- Compute AD (absolute difference) between every overlaid pair of pixels
- Compute SAD in a window for every pixel

current disparity is *d* = 1

iertiniage										
3	5	4	4	2	4	2				
7	4	1	4	4	2	6				
2	7	46	46	46	6	7				
5	9	46	46	44	9	7				
4	7	47	47	47	2	4				
4	7	56	56	46	6	7				
3	4	4	1	4	3	2				

left image

3	5	4	4	2	4	2
7	4	1	4	4	2	6
46	46	46	3	6	6	7
48	46	44	6	4	9	7
47	47	47	7	4	2	4
58	56	46	5	6	6	7
3	4	4	1	4	3	2

right image

AD image for disparity 1

			-		
2	1	0	2	2	2
3	3	З	0	2	0
39	0	0	43	0	0
39	0	2	38	5	0
40	0	0	40	2	0
51	0	10	41	0	0
1	0	3	3	1	0

3	3	5	4	4	2	4	2	
7	7	4	1	4	4	2	6	
2	46	46	46	3	6	6	7	
5	48	46	44	6	4	9	7	
4	47	47	47	7	4	2	4	
4	58	56	46	5	6	6	7	
3	3	4	4	1	4	3	2	

- current disparity is *d* = 1
- Pad AD image with zeros

	lent image										
	3	5	4	4	2	4	2				
	7	4	1	4	4	2	6				
	2	7	46	46	46	6	7				
	5	9	46	46	44	9	7				
	4	7	47	47	47	2	4				
S	4	7	56	56	46	6	7				
	3	4	4	1	4	3	2				

loft imago

3	5	4	4	2	4	2
7	4	1	4	4	2	6
46	46	46	3	6	6	7
48	46	44	6	4	9	7
47	47	47	7	4	2	4
58	56	46	5	6	6	7
3	4	4	1	4	3	2

right image

3	3	5	4	4	2	4	2
7	7	4	1	4	4	2	6
2	46	46	46	3	6	6	7
5	48	46	44	6	4	9	7
4	47	47	47	7	4	2	4
4	58	56	46	5	6	6	7
3	3	4	4	1	4	3	2

AD image	for di	sparity 1
----------	--------	-----------

		U		-		
0	2	1	0	2	2	2
0	3	3	3	0	2	0
0	39	0	0	43	0	0
0	39	0	2	38	5	0
0	40	0	0	40	2	0
0	51	0	10	41	0	0
0	1	0	3	3	1	0

 current disparity is *d* = 1

	3	5	4	4	2	4	2		
	7	4	1	4	4	2	6		
	2	7	46	46	46	6	7		
	5	9	46	46	44	9	7		
	4	7	47	47	47	2	4		
	4	7	56	56	46	6	7		
	3	4	4	1	4	3	2		

left image

3	5	4	4	2	4	2
7	4	1	4	4	2	6
46	46	46	3	6	6	7
48	46	44	6	4	9	7
47	47	47	7	4	2	4
58	56	46	5	6	6	7
3	4	4	1	4	3	2

right image

AD image for disparity 1

				_		
0	2	1	0	2	2	2
0	3	3	3	0	2	0
0	39	0	0	43	0	0
0	39	0	2	38	5	0
0	40	0	0	40	2	0
0	51	0	10	41	0	0
0	1	0	3	3	1	0

current disparity is *d* = 1

			inag	,-		
3	5	4	4	2	4	2
7	4	1	4	4	2	6
2	7	46	46	46	6	7
5	9	46	46	44	9	7
4	7	47	47	47	2	4
4	7	56	56	46	6	7
3	4	4	1	4	3	2

left image

AD image for disparity 1

0	2	1	0	2	2	2
0	3	3	3	0	2	0
0	39	0	0	43	0	0
0	39	0	2	38	5	0
0	40	0	0	40	2	0
0	51	0	10	41	0	0
0	1	0	3	3	1	0

right image

3	5	4	4	2	4	2
7	4	1	4	4	2	6
46	46	46	3	6	6	7
48	46	44	6	4	9	7
47	47	47	7	4	2	4
58	56	46	5	6	6	7
3	4	4	1	4	3	2

 current disparity is *d* = 1

				, 		
3	5	4	4	2	4	2
7	4	1	4	4	2	6
2	7	46	46	46	6	7
5	9	46	46	44	9	7
4	7	47	47	47	2	4
4	7	56	56	46	6	7
3	4	4	1	4	3	2

left image

right image											
3	5	4	4	2	4	2					
7	4	1	4	4	2	6					
46	46	46	3	6	6	7					
48	46	44	6	4	9	7					
47	47	47	7	4	2	4					
58	56	46	5	6	6	7					
3	4	4	1	4	3	2					

AD image for disparity 1

		U			-	
0	2	1	0	2	2	2
0	3	3	3	0	2	0
0	39	0	0	43	0	0
0	39	0	2	38	5	0
0	40	0	0	40	2	0
0	51	0	10	41	0	0
0	1	0	3	3	1	0

- Current disparity is 1
- For each window pixel, have to compute window sums in AD image
- Apply integral image to AD image

AD image for disparity 1

0	2	1	0	2	2	2
0	3	3	3	0	2	0
0	39	0	0	43	0	0
0	39	0	2	38	5	0
0	40	0	0	40	2	0
0	51	0	10	41	0	0
0	1	0	3	3	1	0

Efficient Algorithm for Window Matching

for every pixel <i>p</i> do	A	τΥΙ				
ior every pixer p do	2	1	0	2	2	2
bestDisparity[p] = 0	3	•		-		
bestWindCost[p] = HUGE		3	3	0	4	0
		0	0	43	1	0
for disparity d = 0, 1,, maxD do	39	0	2	38	2	0
overlay images at disparity d	40	0	0	40	2	0
compute AD image for disparity d	51	0	10	41	0	0
compute Integral image from AD image	1	0	3	3	1	0

AD image for disparity 1

for every pixel *p* do

currentCost = window cost at pixel **p**, computed from integral image

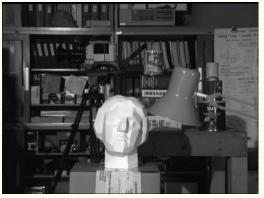
if currentCost < bestWindCost[p]</pre>

bestWindCost[p] = currentCost

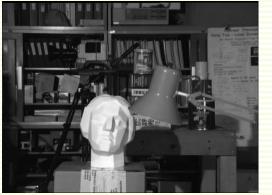
bestDisparity[**p**] = **d**

return bestDisparity

Effect of Window size



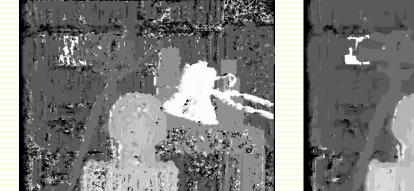
left image



right image



true disparities bright means larger disparity



3x3 window

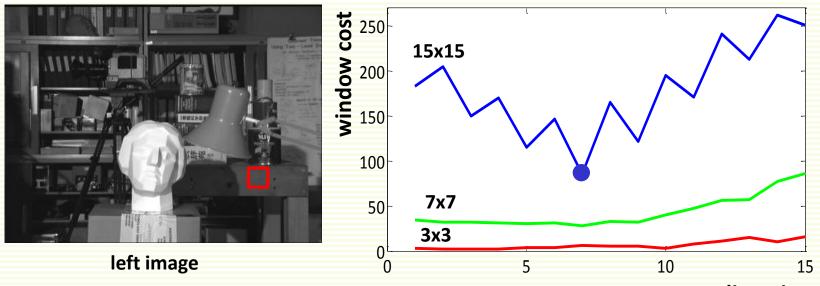




7x7 window

15x15 window

Effect of Window size: Low Texture Area



disparity

- windows of size 3x3 and 7x7 are too small to have a distinct pattern
 - no clearly best disparity
- window of size 15x15 is large enough to have a distinct pattern
 - 7 is clearly the best disparity
- window has to be large enough

Effect of Window size: Near Discontinuities



- central pixel (the one we are matching) is the lamp
- windows of size 3x3 and 7x7 contain mostly the lamp
- window of size 15x15 contains mostly the wall
 - we match the wall instead of the lamp!
- window must be small enough to contain mostly the same object as the central pixel



Effect of Window size

- No single window size is 'perfect' for the image
- Smaller window
 - works better around object boundaries
 - noisy results in low texture areas
- Larger window
 - better results in low texture areas
 - does not preserve object boundaries well
- Adaptive window algorithms exist [Veksler'2001]





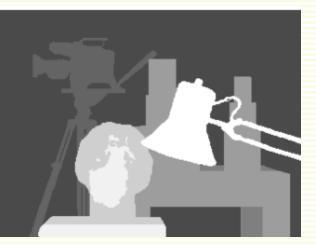




Better Stereo Algorithms



State of the art method [Boykov, Veksler, Zabih, 2001]

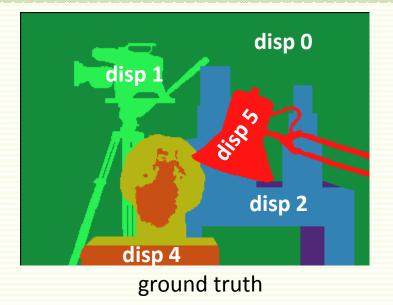


ground truth

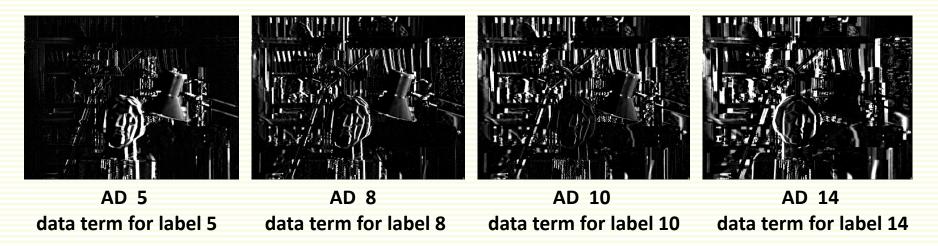
- Formulate stereo as energy minimization
- Recall binary object/background segmentation problem



Better Stereo Algorithms



- Stereo is multi-label segmentation problem
 - region 0 = label 0 "likes" disparity 0
 - region 1 = label 1 "likes" disparity 1
 - ...
 - region maxDisp = label maxDisp "likes" disparity maxDisp



- Energy Function
 - Data Term: assign each pixel disparity label it likes
 - Smoothness Term: count number of label (disparity) discontinuities
- Solved with Graph Cuts: iteratively cuts out regions corresponding to disparities
- NP-hard with more than 2 labels, but computes a good approximation



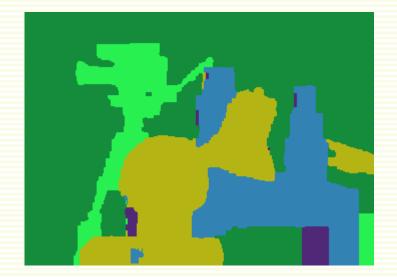
• Start with everything as label (disparity) 0









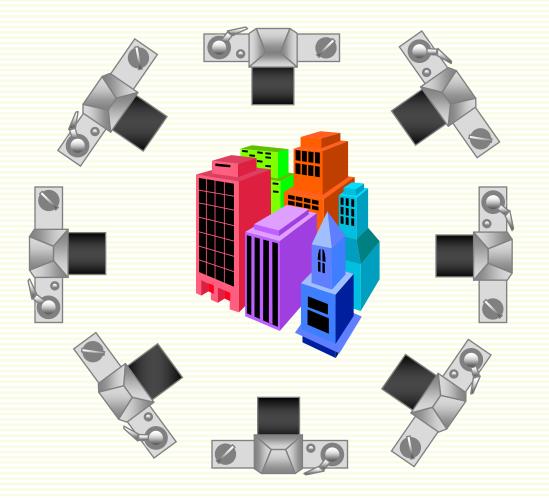




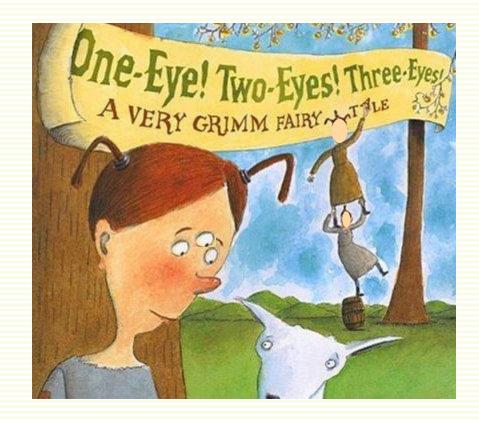


Multiple Artificial Eyes

 Two eyes better than one → three eyes better than two → four eyes better than three → ... → the more, the better



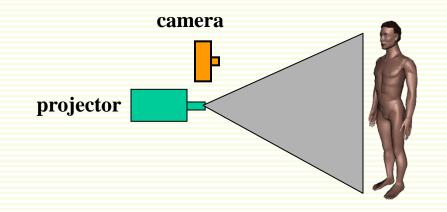
Common Folk New that Already



Stereo with Structured Light

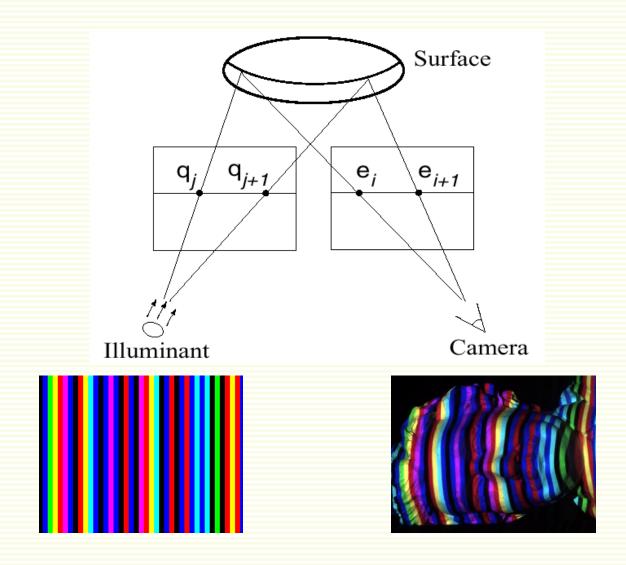


- Project "structured" light patterns onto the object
 - Simplifies correspondence problem
 - Need one camera and one projector

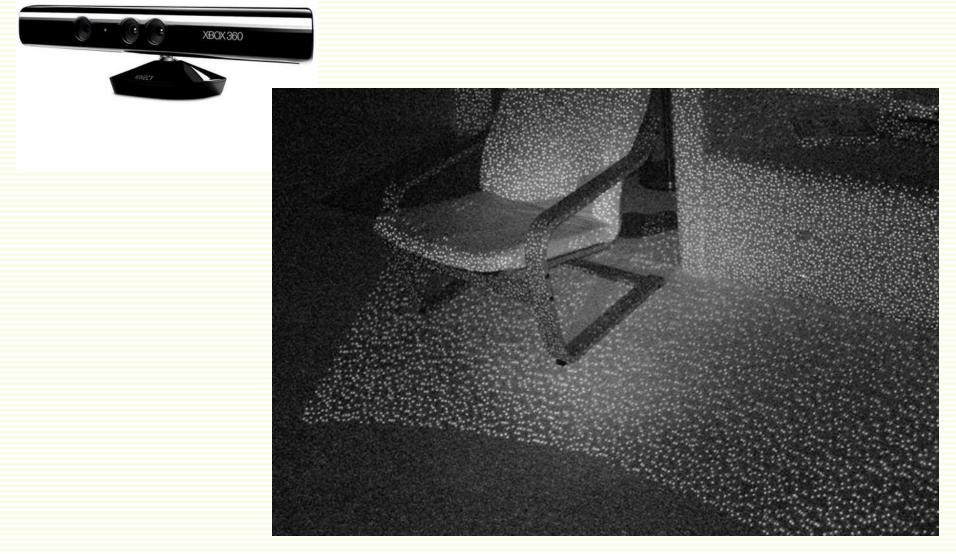


Stereo with Structured Light

Triangulate between camera and projector

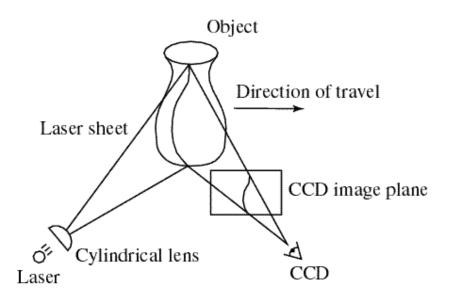


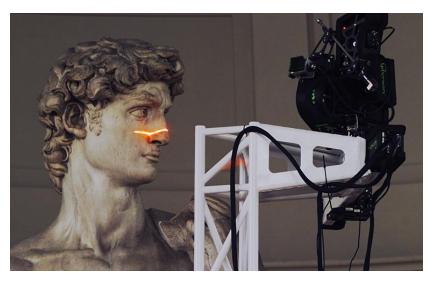
Kinect: Structured Infrared Light



http://bbzippo.wordpress.com/2010/11/28/kinect-in-infrared/

Laser Scanning





Digital Michelangelo Project Levoy et al. http://graphics.stanford.edu/projects/mich/

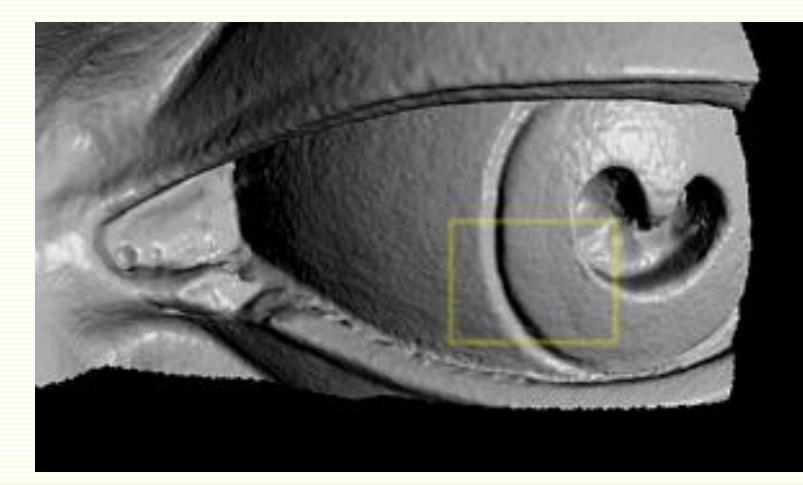
- Optical triangulation
 - Project a single stripe of laser light
 - Scan it across the surface of the object
 - This is a very precise version of structured light scanning

Laser Scanned Models



The Digital Michelangelo Project, Levoy et al.

Laser Scanned Models



The Digital Michelangelo Project, Levoy et al.

Numerous Applications

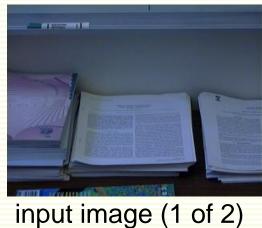
Autonomous navigation



Nomad robot searches for meteorites in Antartica

http://www.frc.ri.cmu.edu/projects/meteorobot/index.html

Novel View Synthesis







3D rendering

) depth map [Szeliski & Kang '95]

Applications: Video View Interpolation

http://research.microsoft.com/users/larryz/videoviewinterpolation.htm



Stereo Correspondence

- Steps:
 - Calibrate cameras
 - Rectify images
 - Stereo correspondence
 - Apply depth/disparity formula
- Stereo correspondence is still heavily researched
- The simple window matching algorithm we studied is heavily used in practice due to speed and simplicity
- Popular Benchmark http://www.middlebury.edu/stereo